



*Beyond Einstein: From the Big Bang to Black Holes*

# *Achieving the Very Low End of the LISA Sensitivity Band*

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NASA/GSFC

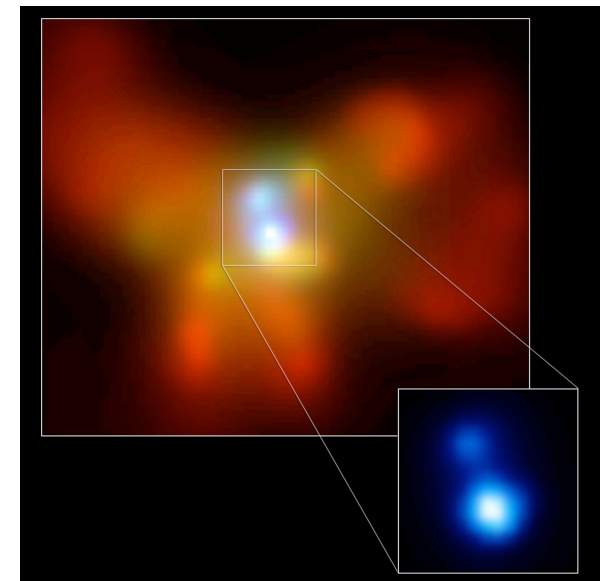
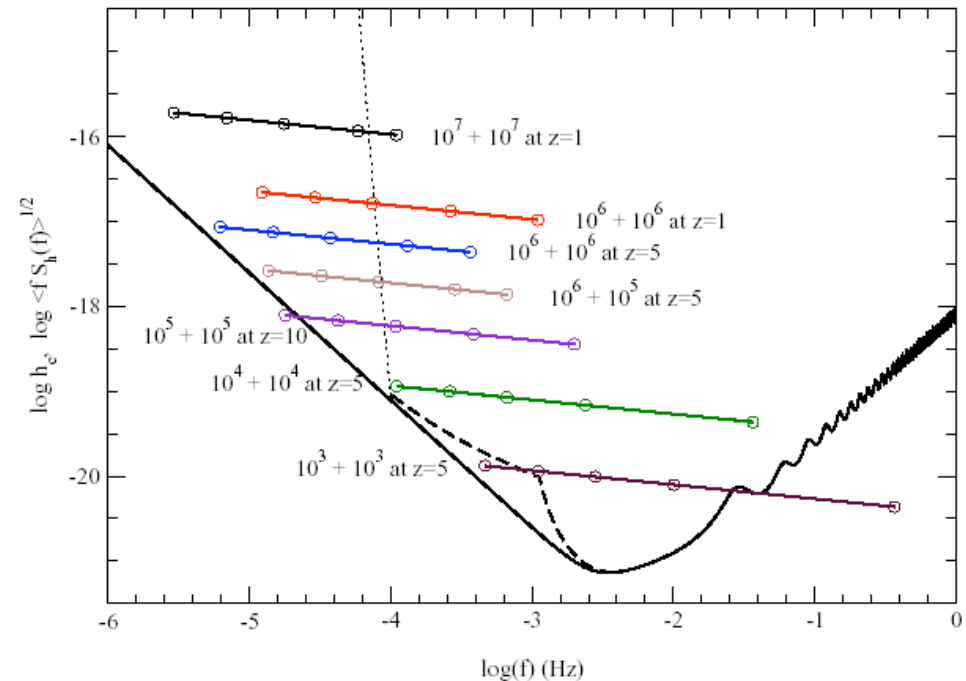
June 20, 2006



# Low Frequency Science

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- Massive black holes are believed to be at the center of all galaxies with bulges.
- Typical galaxies are believed to have at least one merger.
- Gravitational waves from final merger are detectable by LISA to high  $z$  ( $\sim 20$ )
- Expect multiple events per year within LISA sensitivity.
- Observations of such events by LISA:
  - Can be used to map merger history of MBHs (and their host structures) to high  $z$ ,
  - Provide tests of strong GR dynamics.
- Better low-frequency sensitivity:
  - Better distance resolution,
  - Longer integration time  $\rightarrow$  better angular resolution,
  - More secure sources.



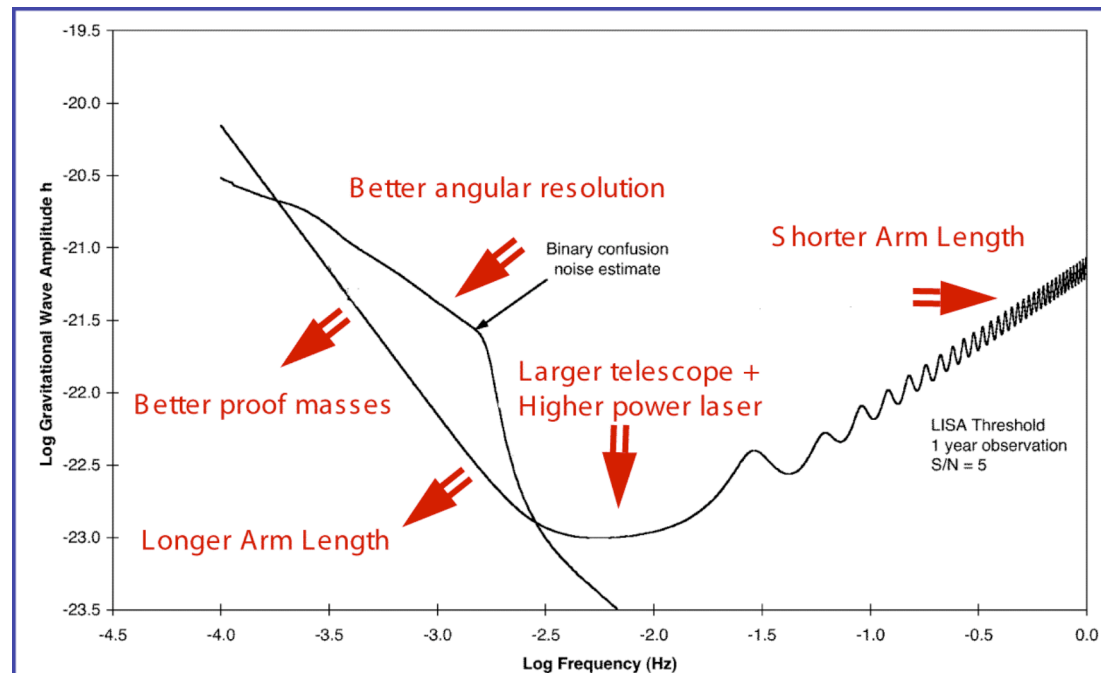
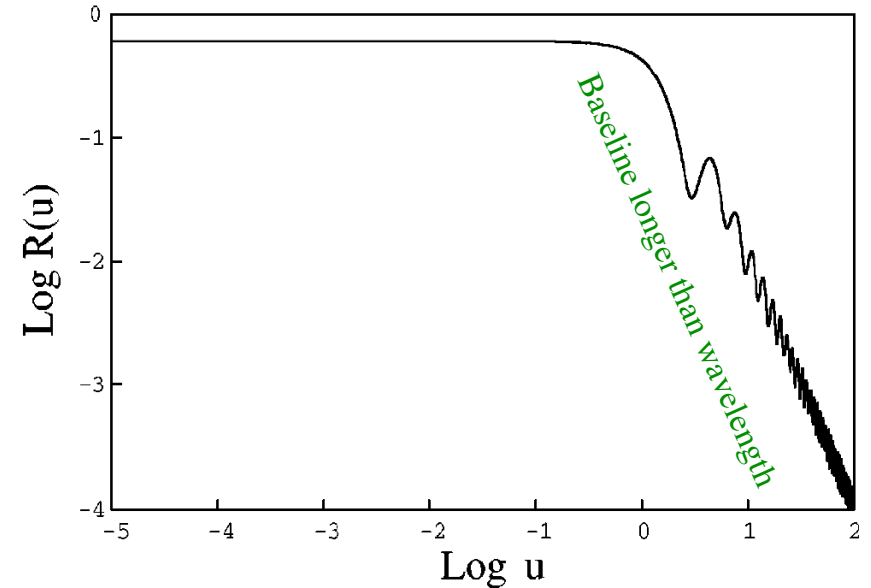
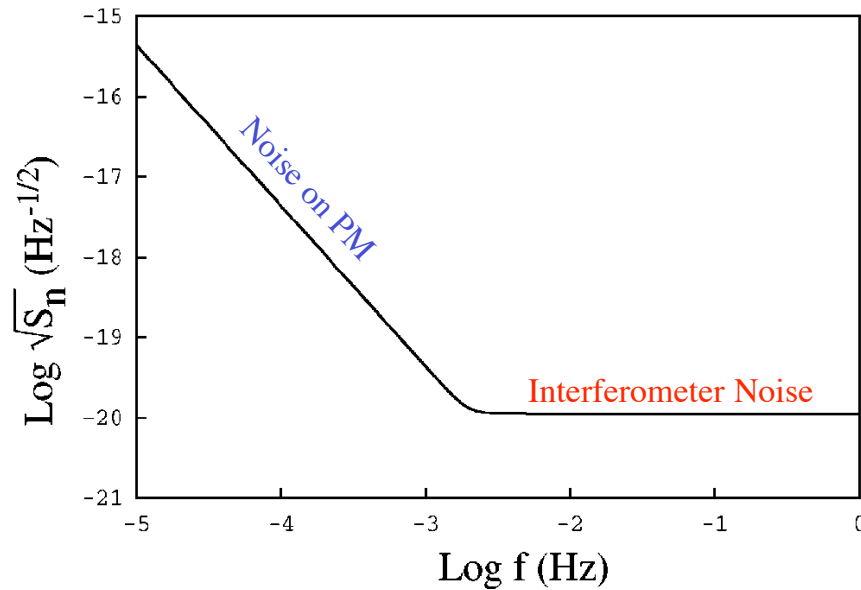




# LISA

# LISA Frequency Response

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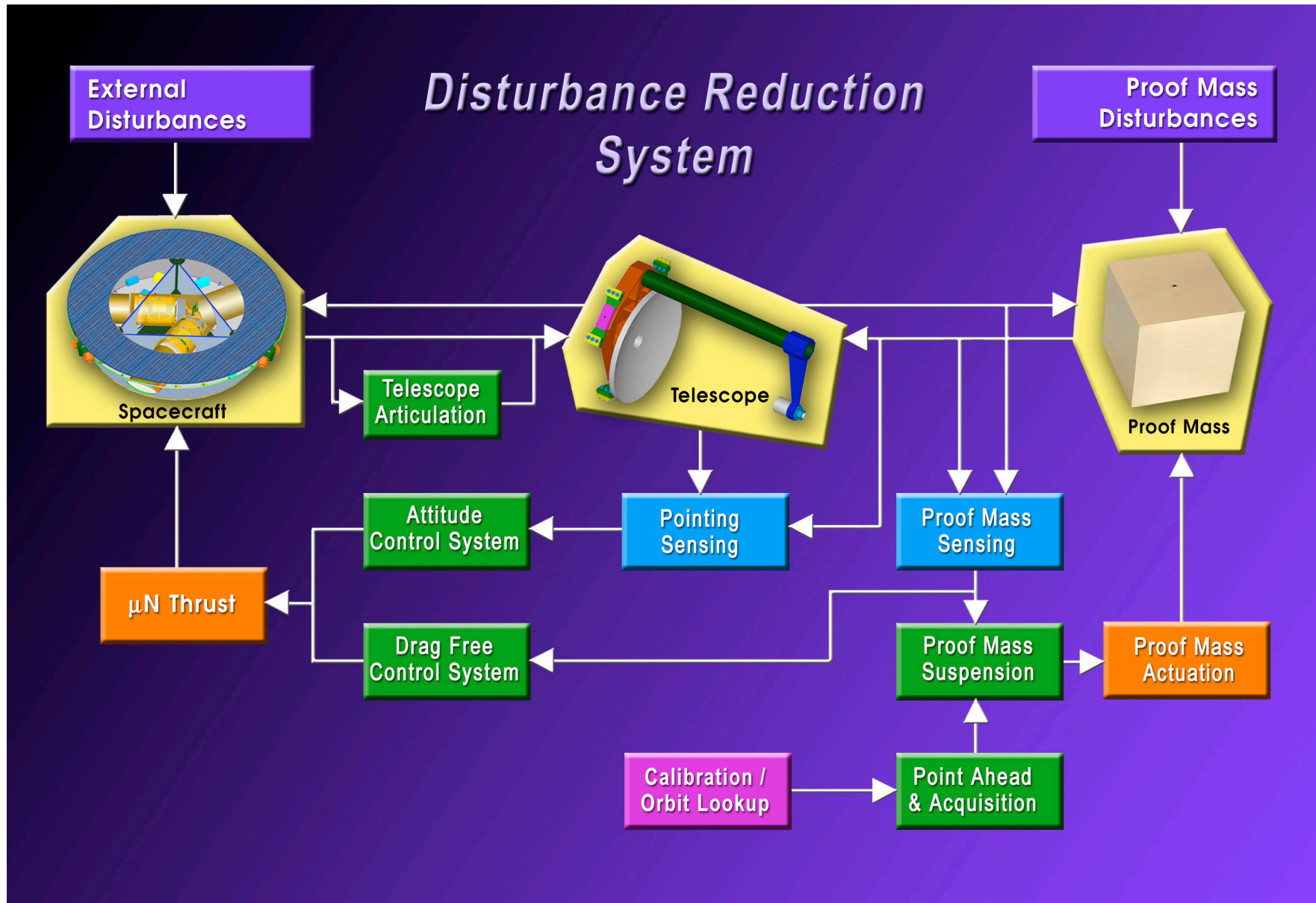




# LISA

## Disturbance Reduction System (DRS)

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# LISA

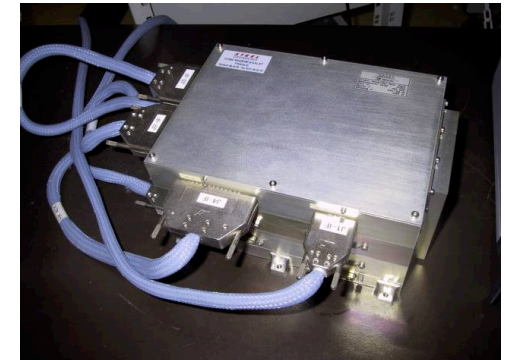
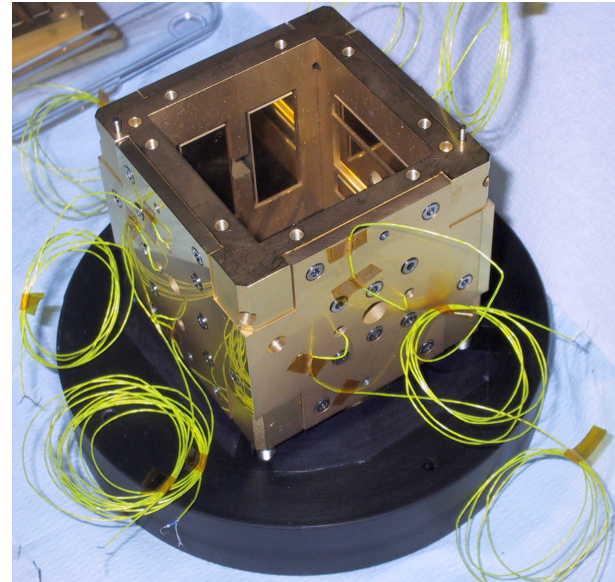
# Disturbance Reduction Technology

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## Gravitational sensor

- Two GRS's on each LISA S/C.
- The LISA GRS will fly on LPF
- Ground development of Pathfinder GRS complete.
- GRS EM successfully passed thermal-vac and vibration testing.



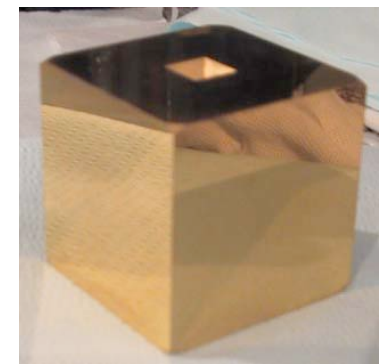
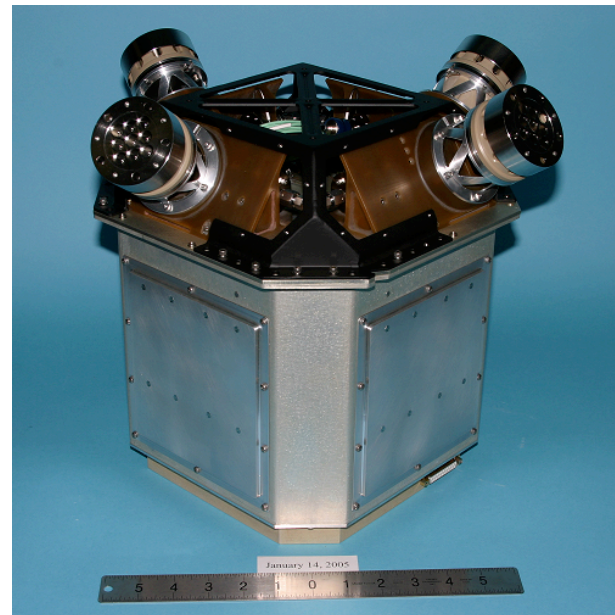
## Microthrusters

- European FEEPs will fly on LPF
- US electro spray (colloid) thrusters will fly on LPF



## Control System

- 57 DOFs
- Drag-free control similar to LISA configuration will be demonstrated on LPF.

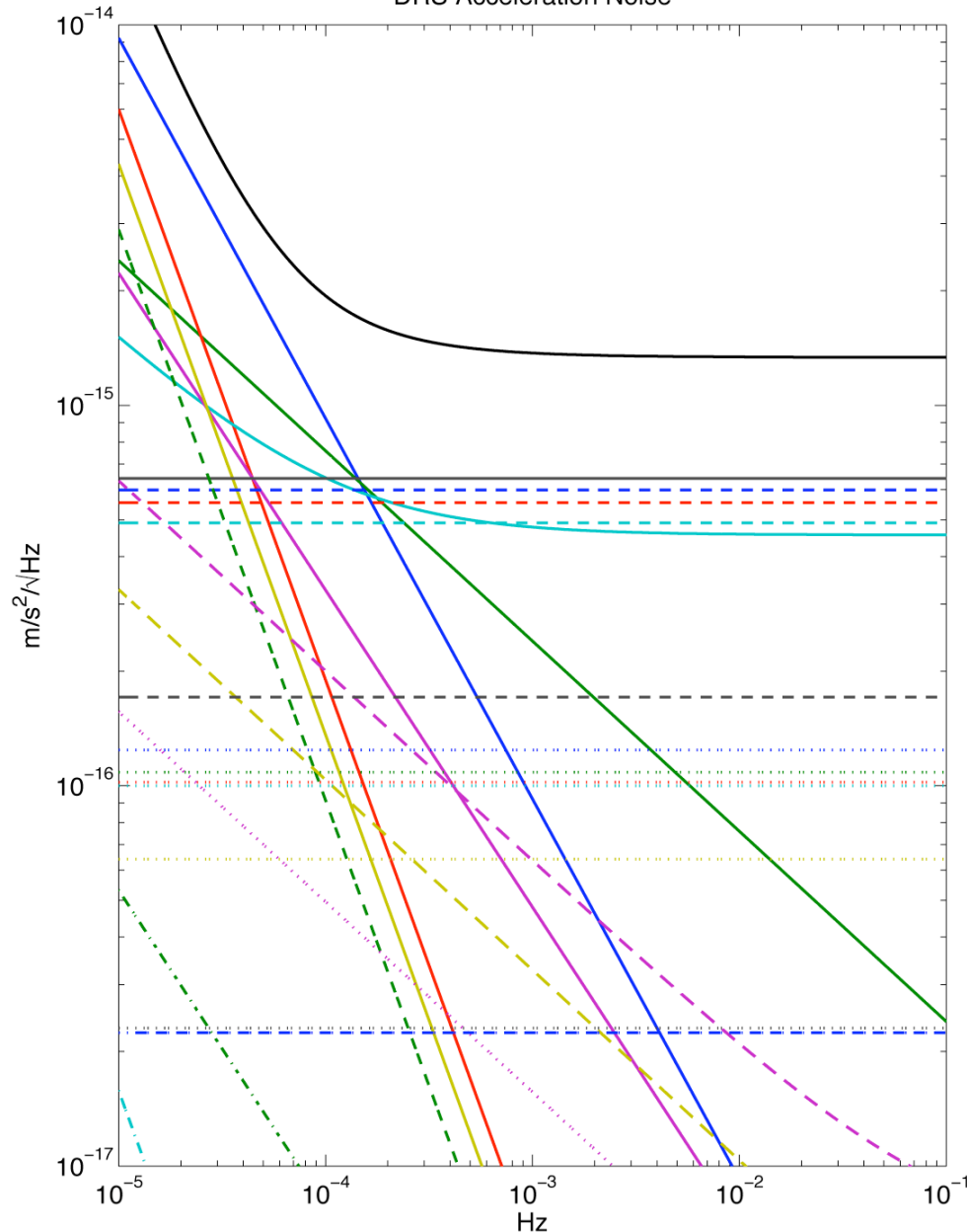




# DRS Acceleration Noise Model

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DRS Acceleration Noise



Current DRS noise model includes:

- 50 physical effects

- Steady state PM acceleration
- Steady state PM torque
- PM-S/C coupling (stiffness)
- Direct PM acceleration noise

- 123 physical parameters

Available parameter values:

- Budgeted
- Current best estimate
- Goal/optimistic



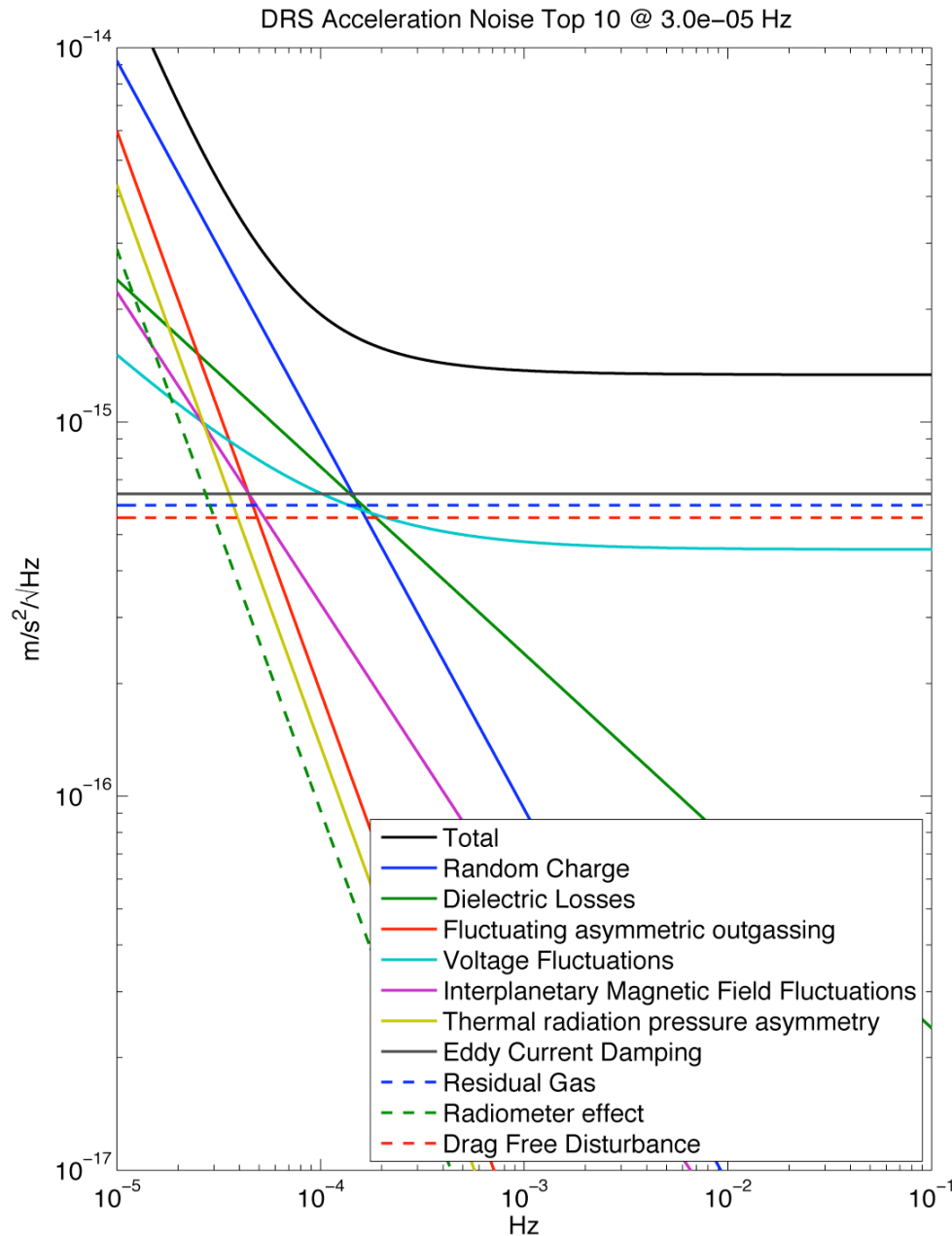


# LISA

## Top 10 Effects at 0.03 mHz

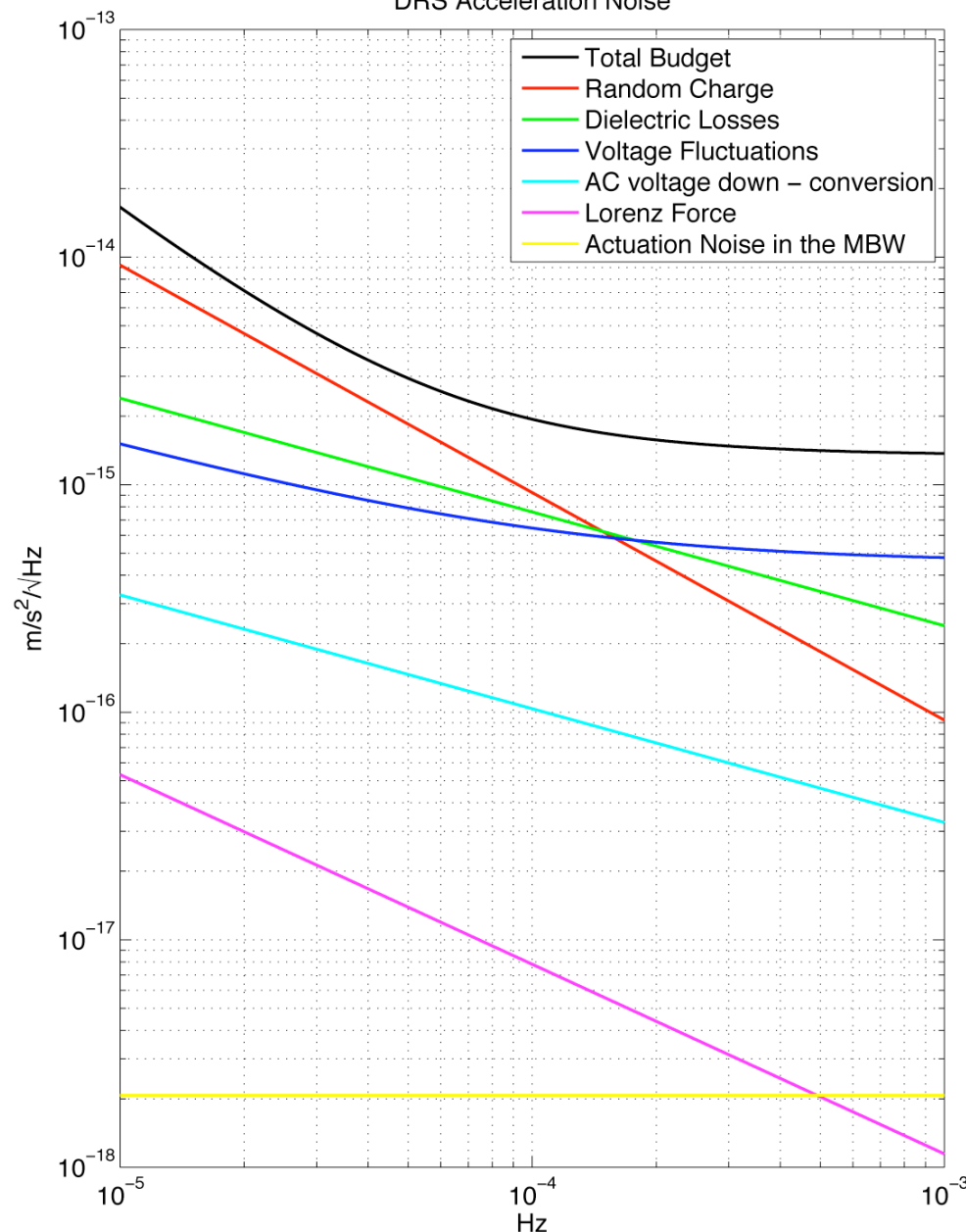


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- Charge & voltage effects
- Thermal effects
- Magnetic effects
- Spacecraft to proof mass coupling

DRS Acceleration Noise



## Random Charge

- Fluctuating PM charge coupled to DC field.



## Voltage Fluctuations

- In-band fluctuating stray voltages coupled to PM charge and stray DC field.



## Dielectric Losses

- Thermal noise from lossy capacitors.



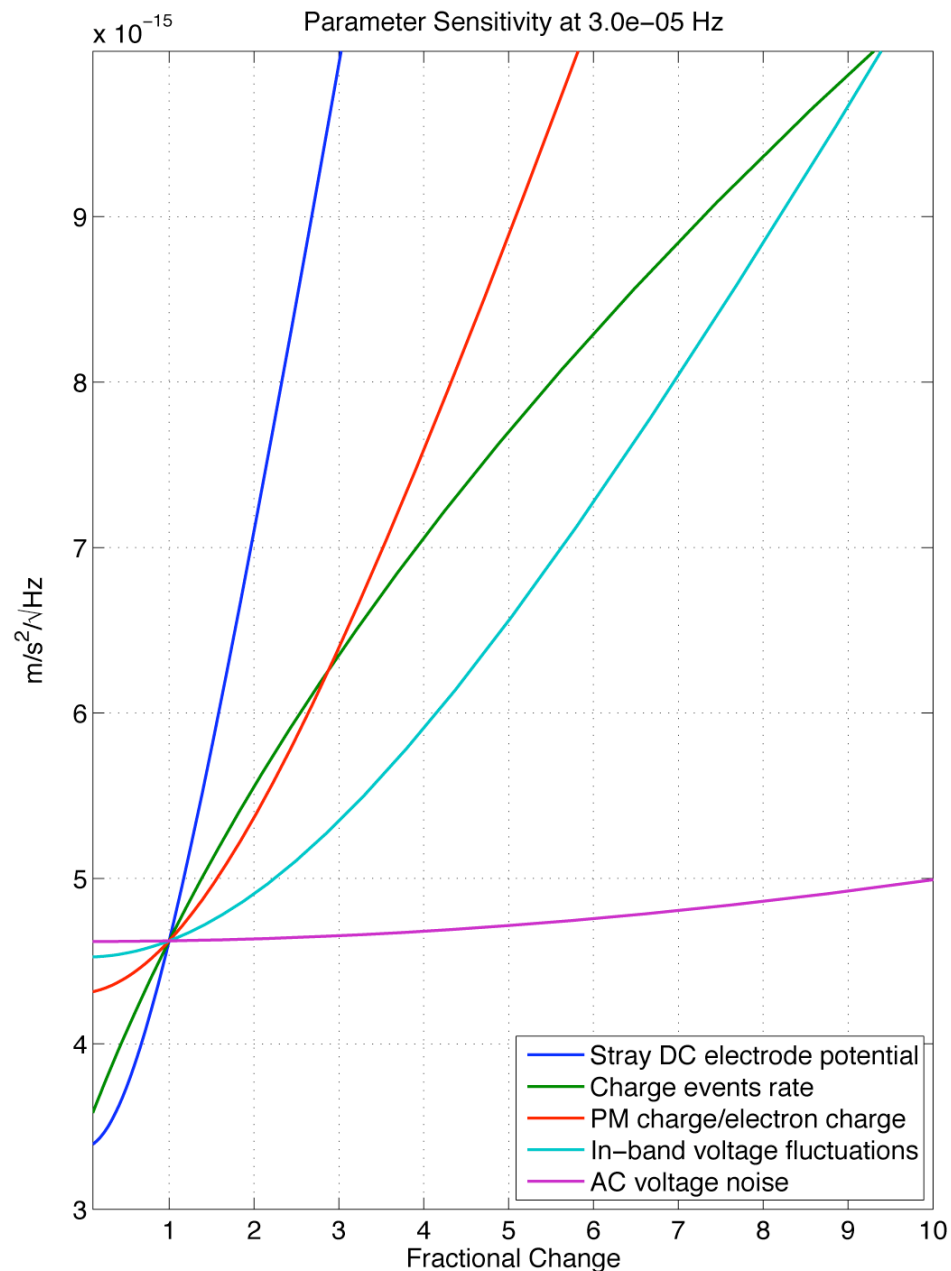
## DC Voltage Stiffness

- PM electrostatic coupling to S/C motion

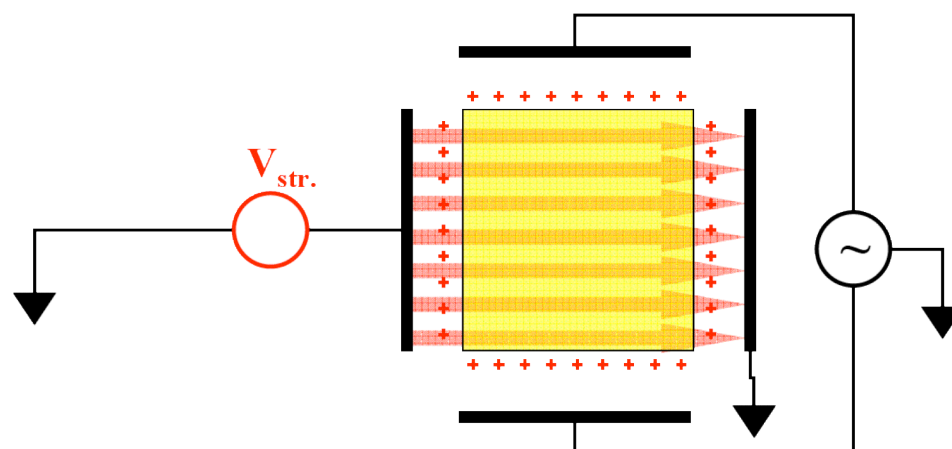


# Voltage & Charge Parameters

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Description	Budget	Units	Sensitivity
Stray DC electrode potential	0.01	V	0.457
Charge events rate	500	1/s	0.222
PM charge/electron charge	$1.0 \times 10^7$		0.120
In-band voltage fluctuations	$2.1 \times 10^{-5}$	$V/\sqrt{Hz}$	0.042
AC voltage noise	$1.8 \times 10^{-7}$	$V/\sqrt{Hz}$	0.002

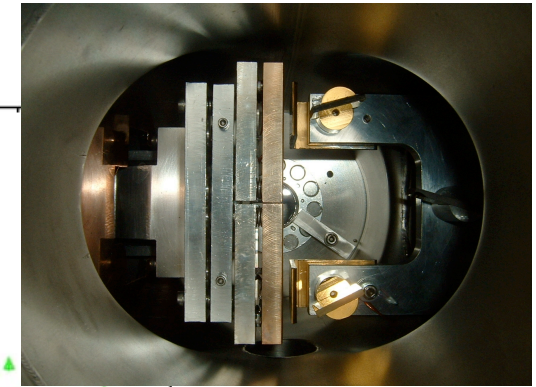
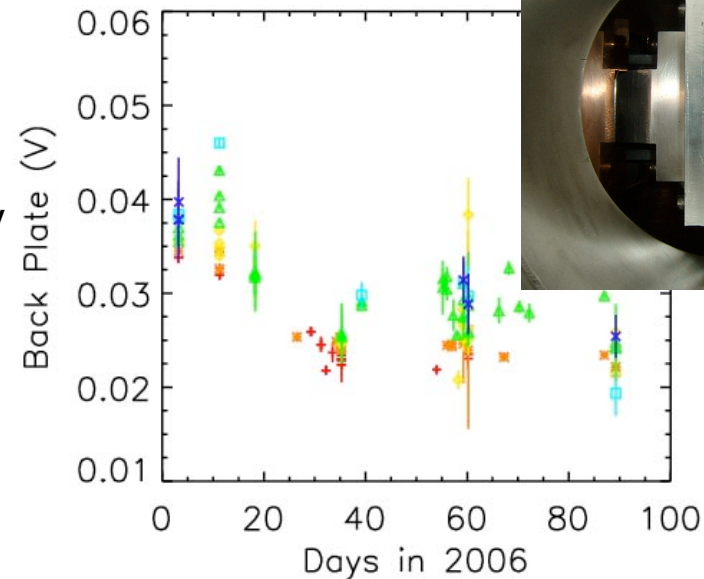




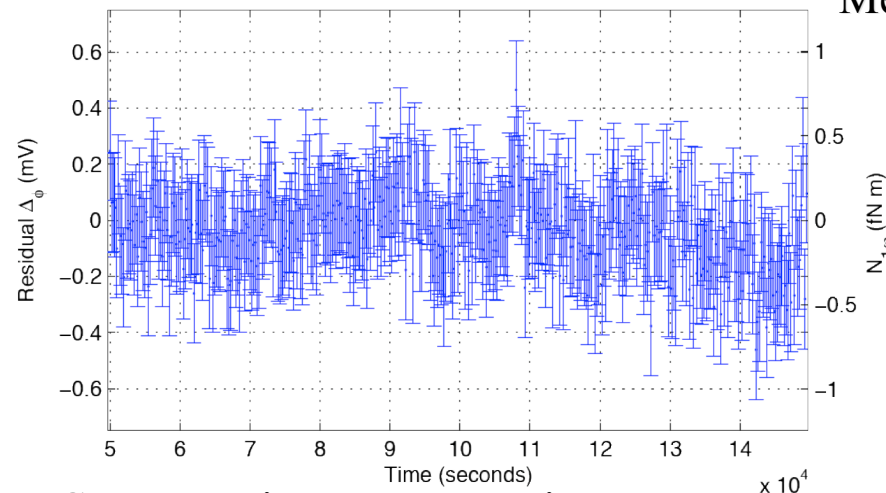
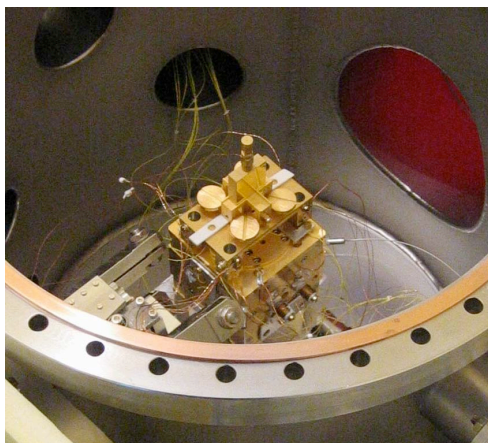
# Stray DC Potential

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- Spatial average of voltage difference from opposite faces.
- Mostly from 'large' patches of spatially varying surface potentials.
- Can be partially compensated by carefully applied electrode voltages.
- Measurements at UW confirm stray DC voltage of ~50 mV.
- Measurements at Trento demonstrate compensation to ~0.5 mV.



UW Small Force Measurements



Trento Voltage Compensation Demonstration

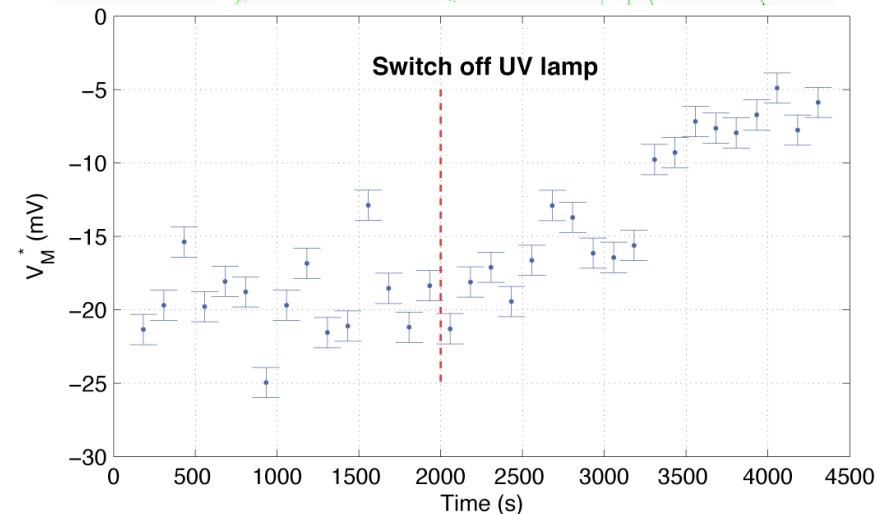
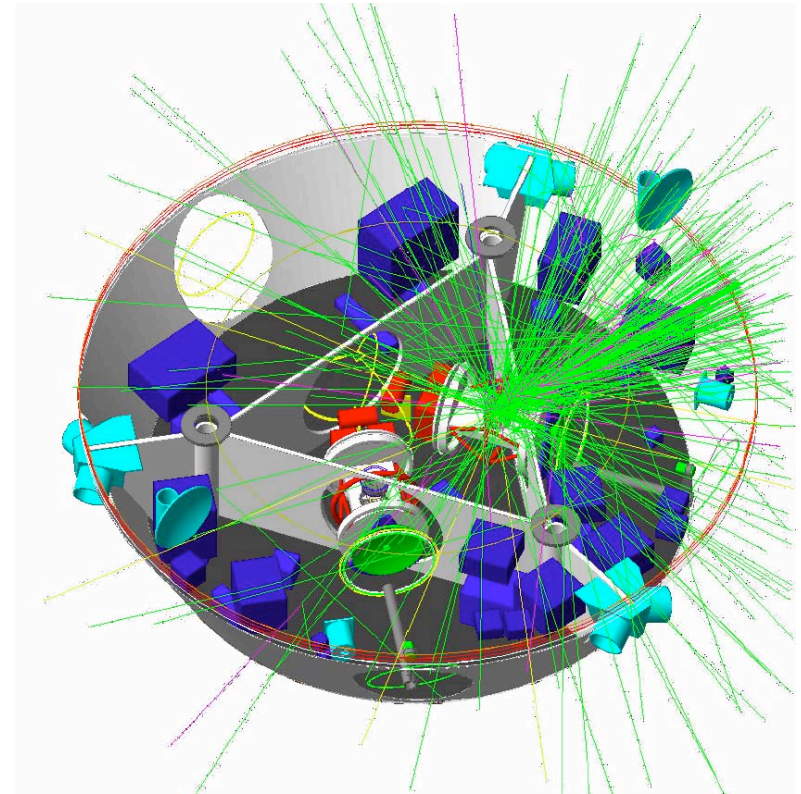




# Proof Mass Charge

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- Cosmic ray impacts will charge the PM.
- Total charge and charge fluctuations will couple to the DC field causing spurious accelerations.
- Charge fluctuations are  $\propto$  to the charging rate:
  - Imperial College GEANT4 model predicts charging rate of  $< 50$  e/s.
  - INFN Fluka model predicts charging rate of 150 e/s.
- Charging rate on GP-B was 8 e/s (Imperial College predicted 12.5 e/s GEANT4).
- Total charge controlled by shining UV light on PM and housing.
  - Measurements at Trento demonstrate charge reduction to  $\sim 5 \times 10^6$  e (2x lower than budget).



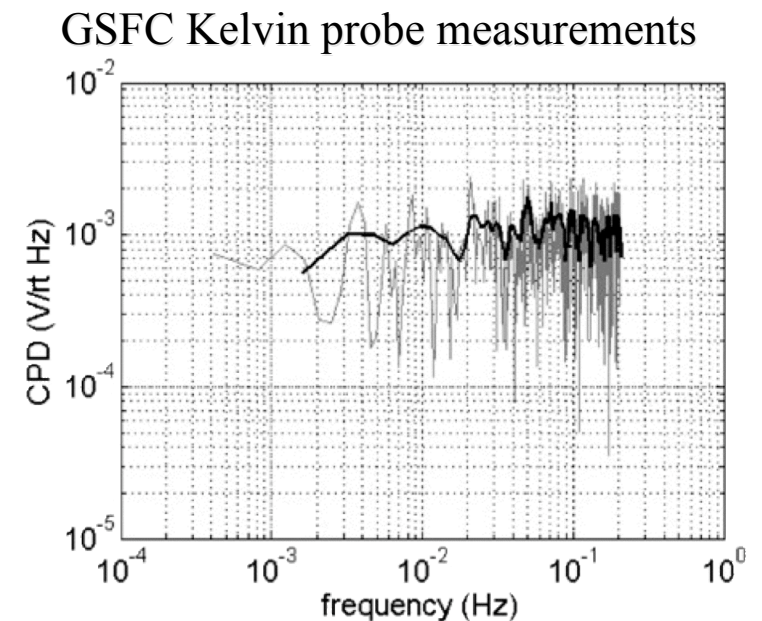
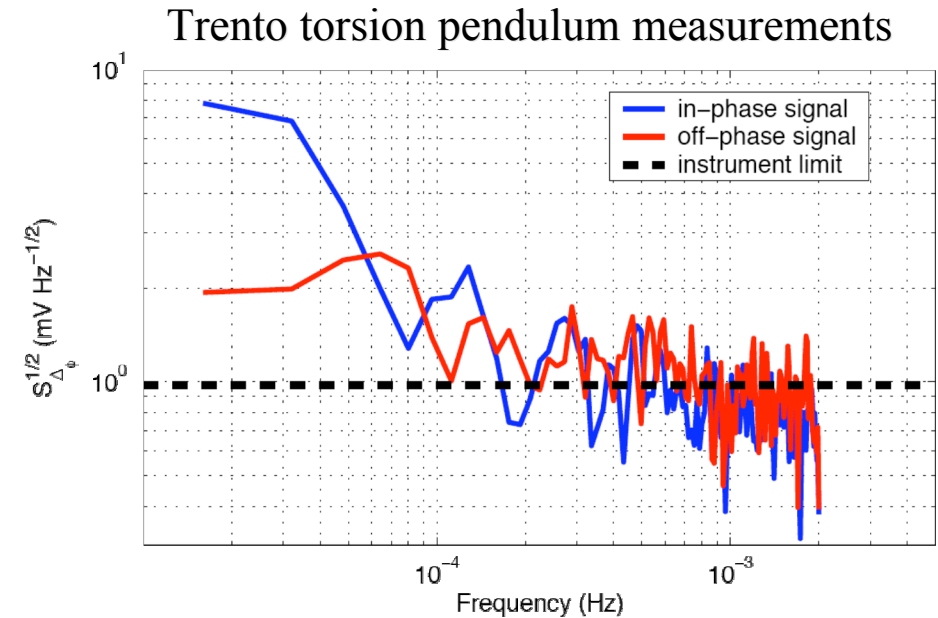
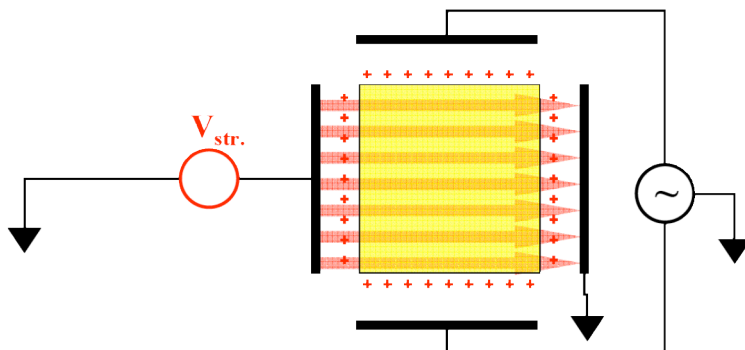


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## Voltage Fluctuations

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- DC field will fluctuate due to:
  - Changing patch fields,
  - Noise in applied voltages.
- Voltage fluctuations will couple to PM charge and stray DC potential:
  - Measurements at Trento put upper limit at  $\sim 1 \text{ mV}/\sqrt{\text{Hz}}$  at 0.1mHz,  $\sim 100\times$  budget value.
  - Measurements on GSFC Kelvin probe put upper limit at  $\sim 1 \text{ mV}/\sqrt{\text{Hz}}$  at 0.4mHz.



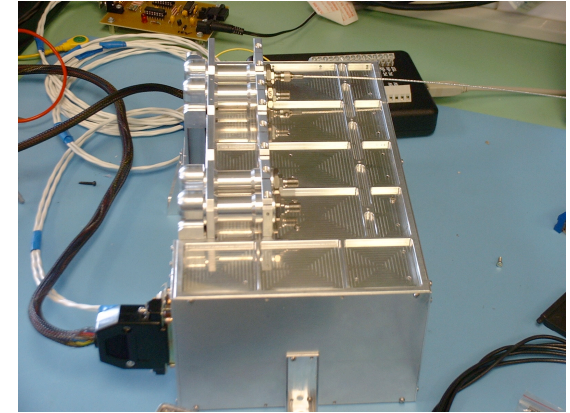


# LISA

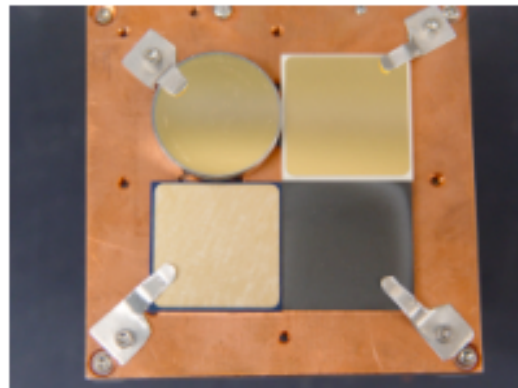
## Achieving Charge & Voltage Performance

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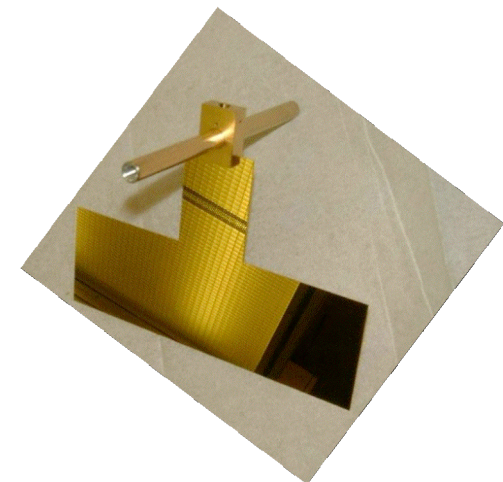
- ❶ Wide gap between PM and housing,
- ❷ No applied DC voltages along sensitive axis,
- ❸ Stray DC voltage active compensation,
- ❹ High quality surface coatings,
- ❺ High stability power supplies,
- ❻ Continuous UV discharging of proof mass.



LTP UV Lamp



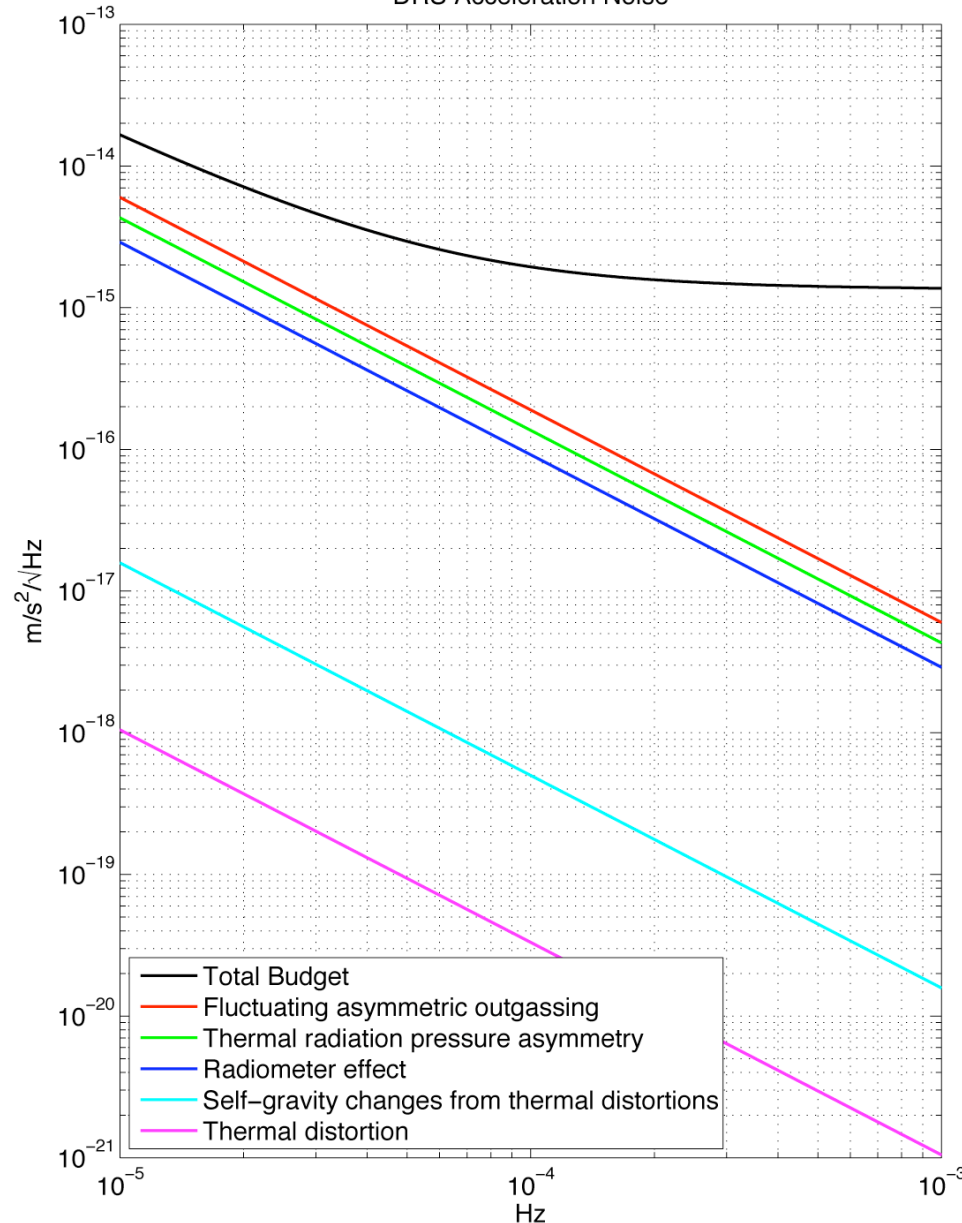
Material samples for Kelvin probe



UW Small Force Pendulum

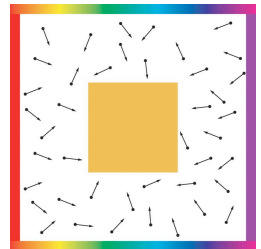


DRS Acceleration Noise



## Fluctuating asymmetric outgassing

- Fluctuating pressure due to temperature dependent outgassing



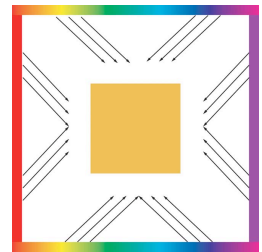
## Radiometer effect

- Fluctuating temperature gradient of residual gas



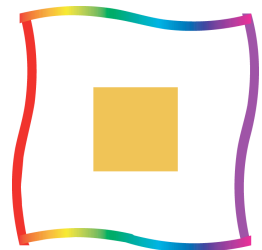
## Thermal radiation pressure asymmetry

- Fluctuating blackbody radiation from EH



## Thermal distortion

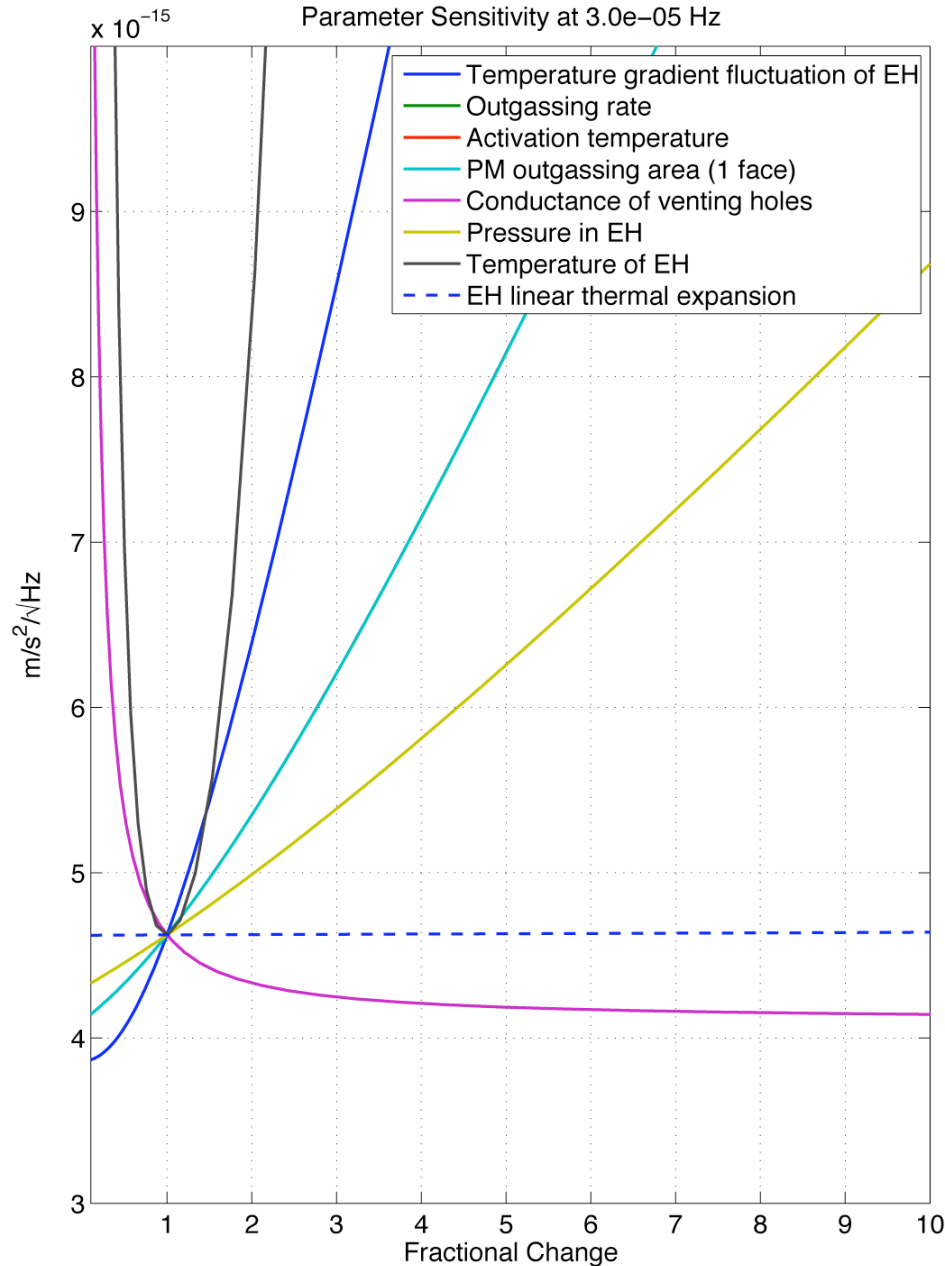
- Housing distortion that couple to PM through self-gravity and capacitance changes.



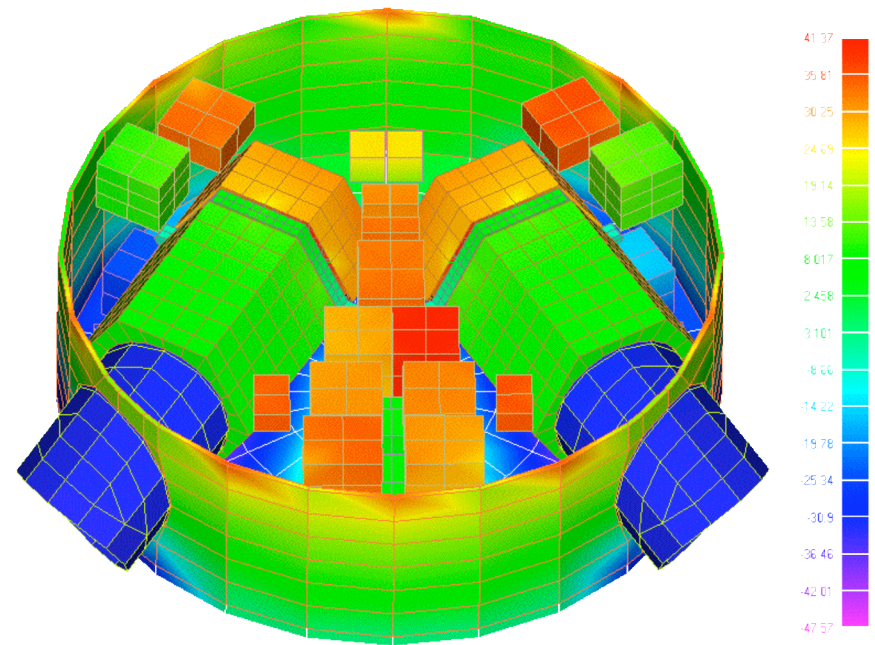


# Thermal Parameters

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Description	Budget	Units	Sensitivity
Temperature gradient fluctuation of EH	$6.1 \times 10^{-5}$	K/ $\sqrt{\text{Hz}}$	0.304
Outgassing rate	$5.0 \times 10^{-7}$	kg/s <sup>3</sup>	0.138
Activation temperature	$3.0 \times 10^4$	K	0.138
Conductance of venting holes	$4.3 \times 10^{-3}$	m <sup>3</sup> /s	0.138
Pressure in EH	$1.0 \times 10^{-5}$	Pa	0.075
Temperature of EH	293	K	0.014
EH linear thermal expansion	$5.0 \times 10^{-6}$	1/K	0.000

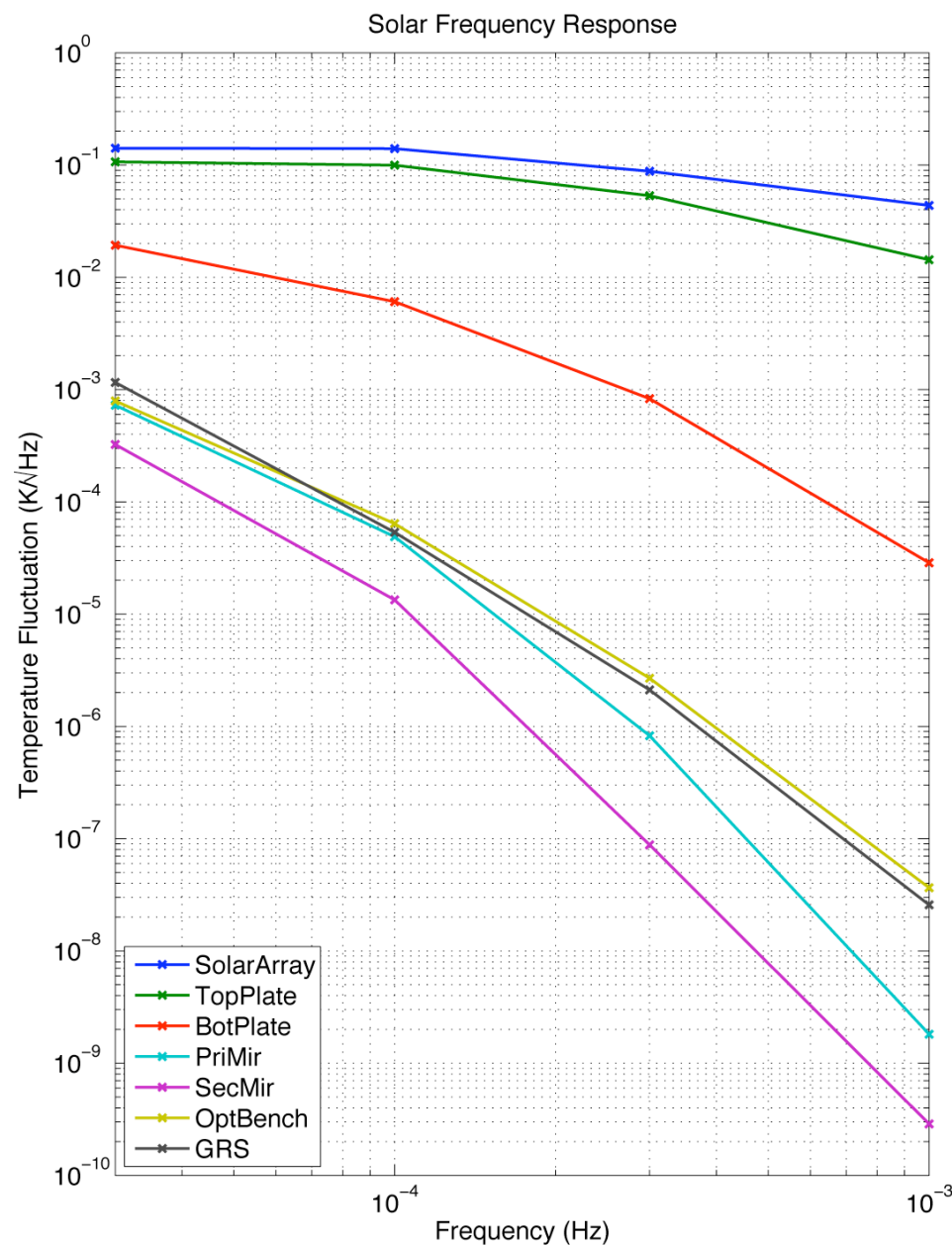
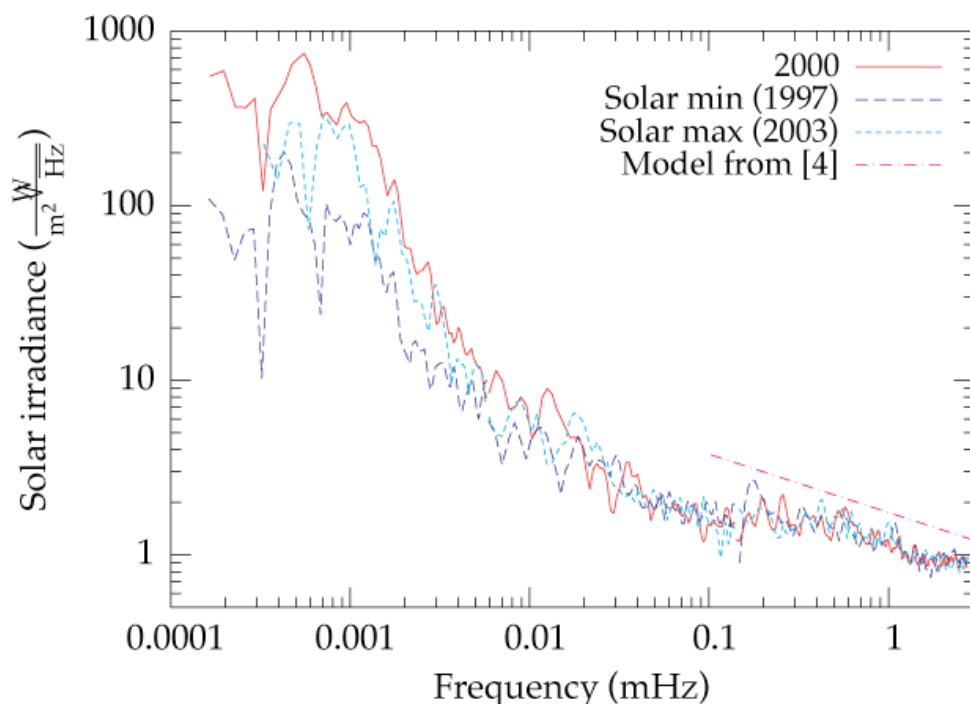




# Thermal Stability

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- Thermal fluctuations come from solar input and electronics.
- Current S/C design has several layers of thermal isolation.
- Thermal modeling indicate  $10 \mu\text{K}/\sqrt{\text{Hz}}$  at 0.1 mHz gradient feasible at GRS.



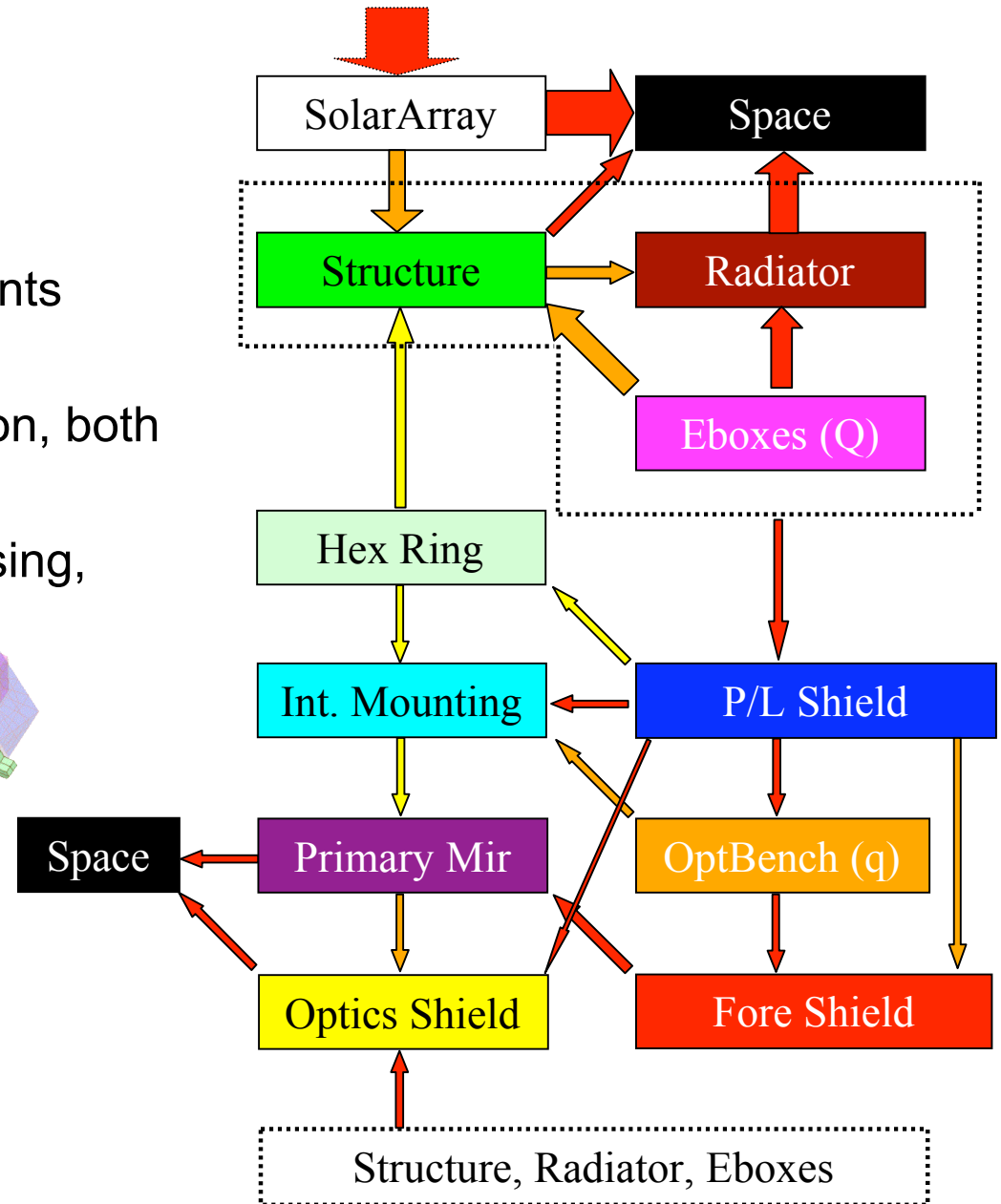
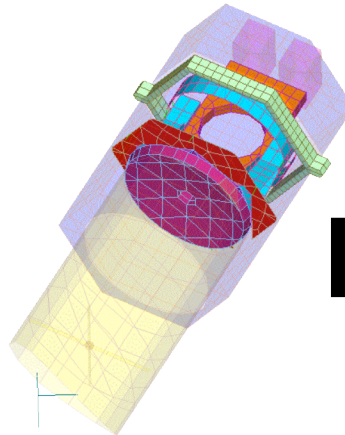
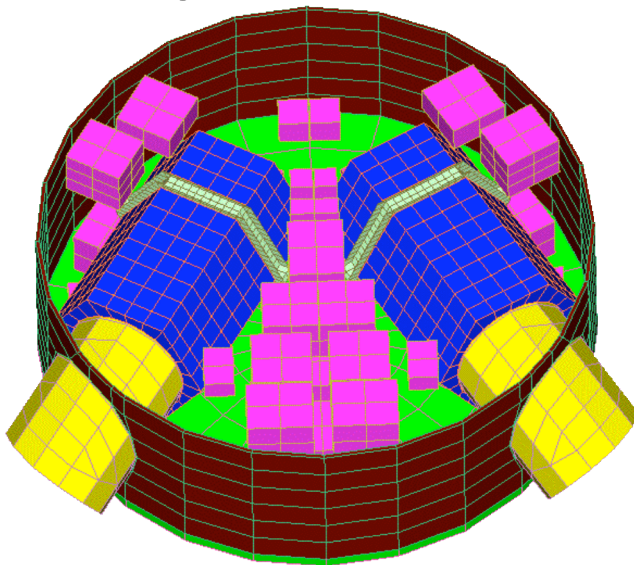


# LISA

## Achieving Thermal Performance

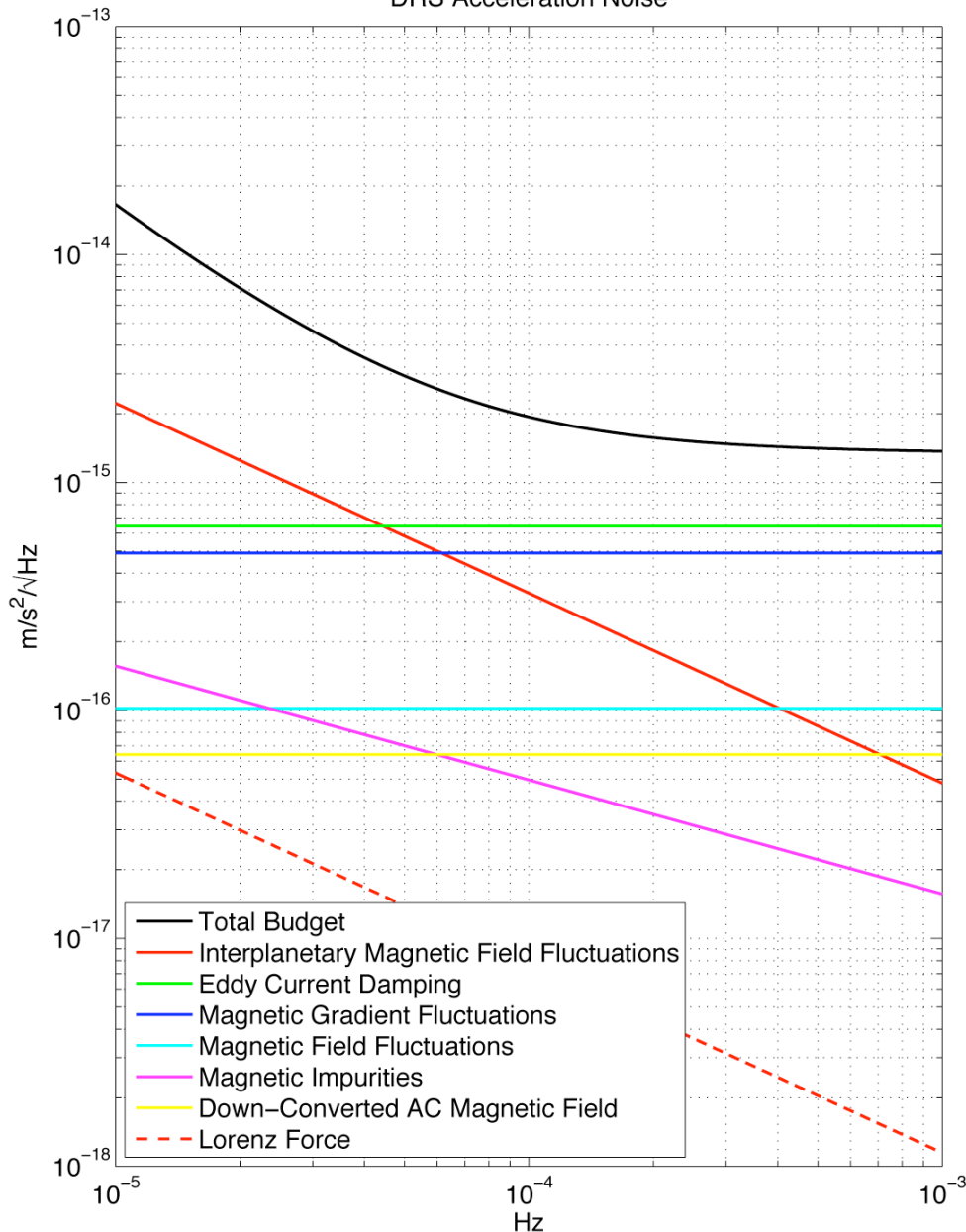
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- Thermally stable environment
  - Constant orientation to sun,
  - Zero Earth/Albedo
- Power Stabilized electrical components (constant dissipation),
- Descending layers of thermal isolation, both conductive and radiative,
- Thermally conductive electrode housing,
- High vacuum.





DRS Acceleration Noise



- Interplanetary magnetic field fluctuations:
  - Interaction between IP magnetic field with S/C magnetic gradient and PM magnetic susceptibility.
- Eddy current damping:
  - Fluctuations from magnetic gradient induced current dissipations.
- Magnetic gradient fluctuations:
  - Interaction between fluctuating S/C magnetic gradient and PM magnetic susceptibility and residual dipole moment.

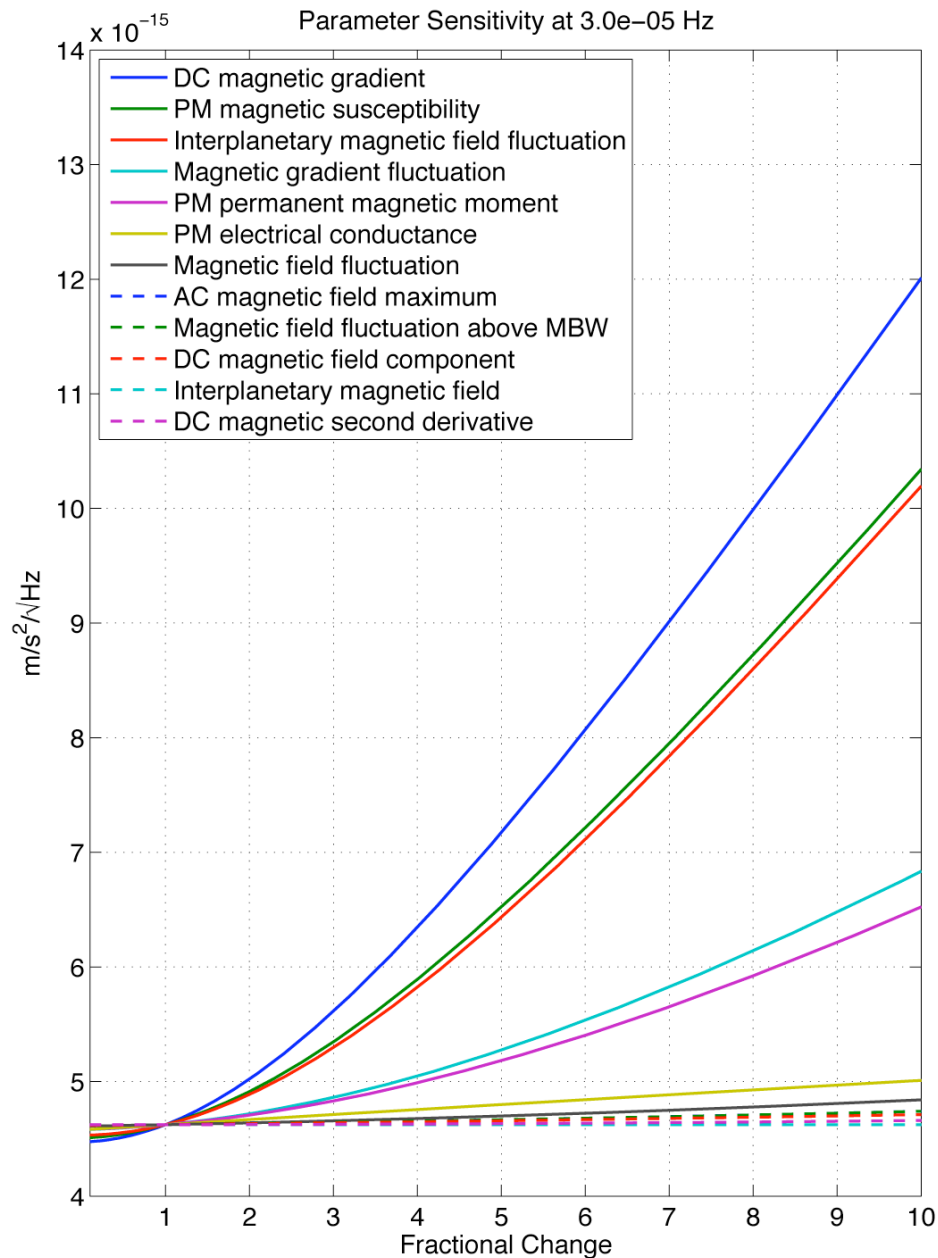




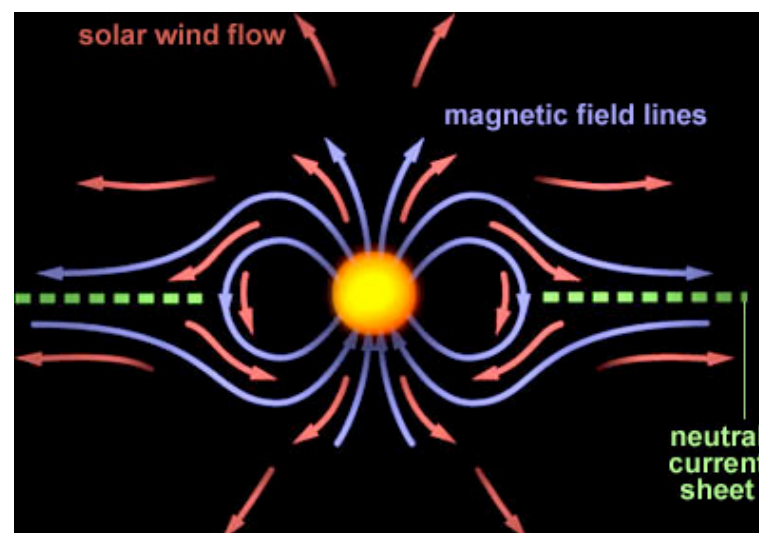


# Magnetic Parameters

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Description	Budget	Units	Sensitivity
DC magnetic gradient	$5.0 \times 10^{-6}$	T/m	0.061
PM magnetic susceptibility	$3.0 \times 10^{-6}$		0.045
Interplanetary magnetic field fluctuation	$8.7 \times 10^{-7}$	T/ $\sqrt{\text{Hz}}$	0.039
Magnetic gradient fluctuation	$2.5 \times 10^{-8}$	T/m/ $\sqrt{\text{Hz}}$	0.015
PM permanent magnetic moment	$2.0 \times 10^{-8}$	A m <sup>2</sup>	0.014
PM electrical conductance	$5.0 \times 10^{-8}$	A/V/m	0.010
Magnetic field fluctuation	$1.0 \times 10^{-7}$	T/ $\sqrt{\text{Hz}}$	0.003
AC magnetic field maximum	$5.0 \times 10^{-7}$	T	0.002
Magnetic field fluctuation above MBW	$1.0 \times 10^{-8}$	T/ $\sqrt{\text{Hz}}$	0.002
DC magnetic field component	$1.0 \times 10^{-5}$	T	0.002
Shielding factor	$1.0 \times 10^{-3}$		0.001
Interplanetary magnetic field	$3.0 \times 10^{-8}$	T	0.000
DC magnetic second derivative	$2.0 \times 10^{-1}$	T/m <sup>2</sup>	0.000



- Levels required by LISA are more than 10x easier than magnetically clean spacecraft.
- Magnetic gradients come mostly from:
  - Strong magnetic materials
  - Soft magnetic materials
  - Currents
- Magnetic zones can be set up to take advantage of  $r^4$ .

$$\mu = \frac{2\pi}{3\mu_0} r^4 \max(B_{xx})$$

- $B_{xx} = 1 \times 10^{-6}$  T/m is equivalent to 20 J/T dipole 1.86 m away.
- Current watch list meets requirements with modest shielding.

Component	Quantity	Dipole (J/T)
HGA Drive Mechanism	2	
Transponders	2	
RFDU	1	
Heaters	Many	
Solar Array	1	
Battery (9A/h LiIon)	1	
Power System Electronics	1	
Power Switching & Distribution Unit (PSDU)	1	
SSPA/TWTA	2	15
Lasers	4	
Isolator	4	10

Magnet Watch List

Zone	Name	Min PM Distance	Max Magnetic Dipole (A-m <sup>2</sup> )
A	Proof masses	0	0
B	Proof mass housings	2	2.70E-12
C	Optical bench	44	6.20E-07
D	Telescope assembly	222	4.00E-04
E	Y-tube outer surface	225	4.30E-04
F	Outside the Y-tube, beyond 250 mm	250	6.50E-04
G	Outside the Y-tube, beyond 500 mm	500	1.00E-02
H	High Gain Antennas	936	1.30E-01
I	Solar array	200	2.70E-04

Magnetic Zones

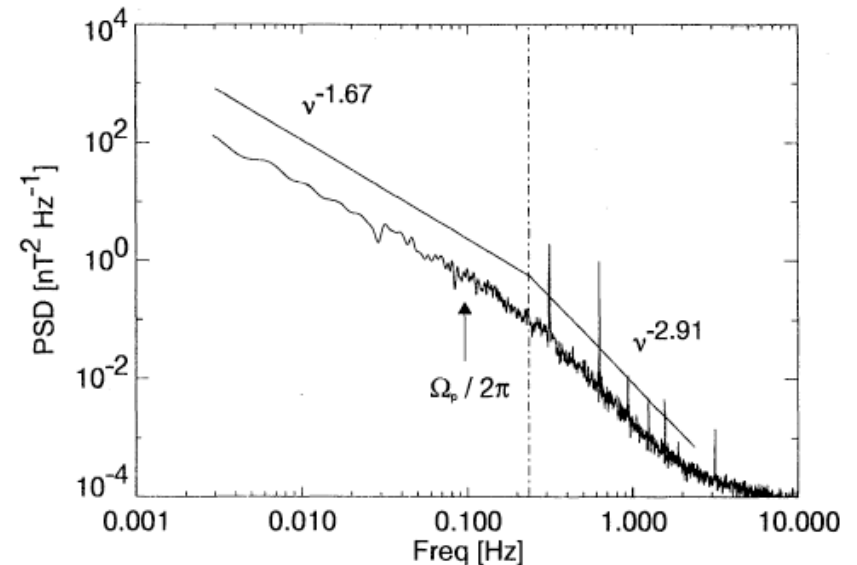
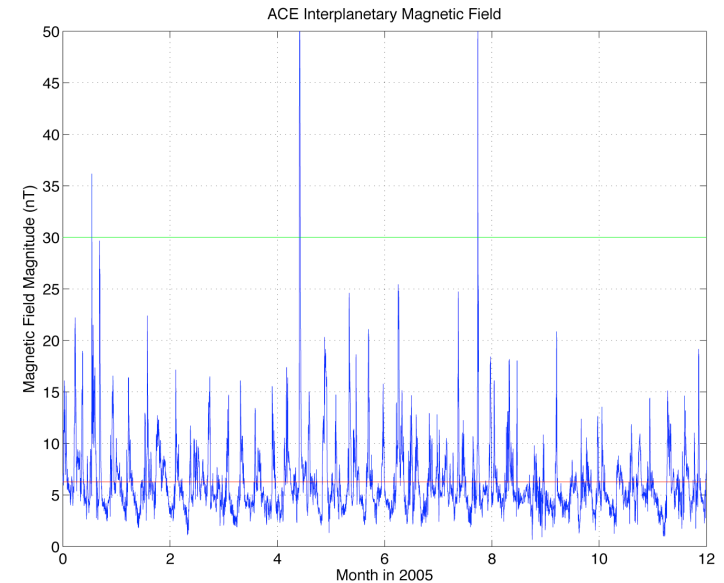


# Interplanetary Magnetic Field

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- Good data exists on interplanetary magnetic field from ACE, Cluster, and other S/C.
- 2005 ACE MAG data has a mean of  $6.3 \pm 3.7$  nT. The value currently assumed in the error budget is 30 nT, more than  $6\sigma$  higher.
- The spectral behavior matches well classical Kolmogorov fluid turbulence, thus the power spectral density of the fluctuations will have an  $f^{-5/3}$  behavior.
- Magnitude of the power spectrum varies considerably. Conservatively assume  $320 \text{ nT}/\sqrt{\text{Hz}}$  at 0.1 mHz.

$$\sqrt{S_{Bi}} = 320 \text{ nT} / \sqrt{\text{Hz}} \sqrt{\left( \frac{10^{-4} \text{ Hz}}{f} \right)^{5/3} \frac{1}{1 + \left( \frac{f}{0.44 \text{ Hz}} \right)^3}}$$

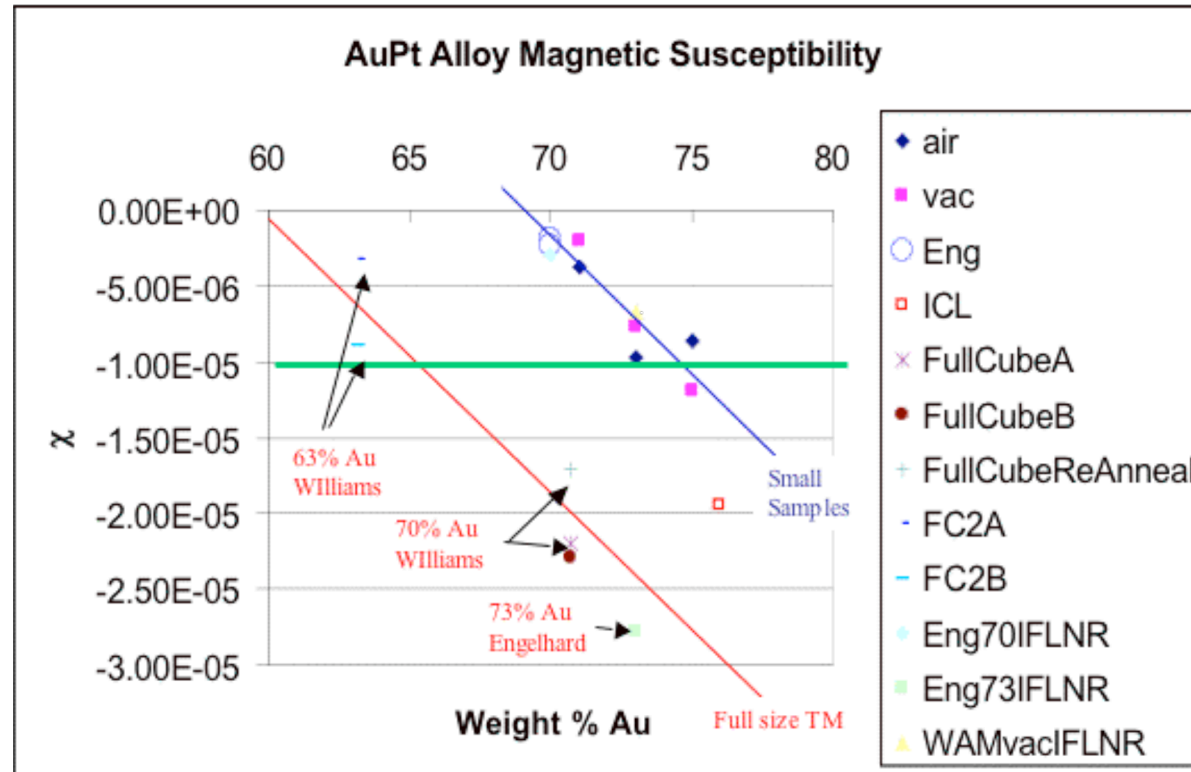


R. Leamon *et al.*, J. Geophys. Res. **104**, 22331 (1999).

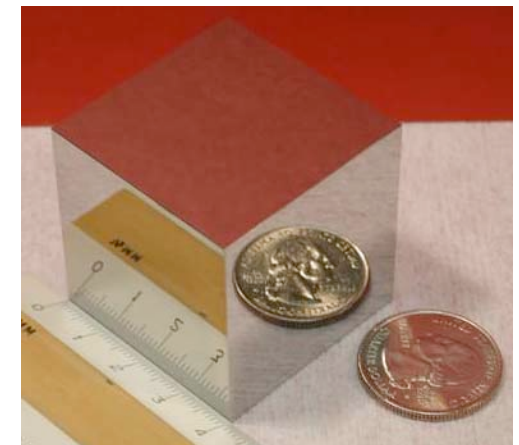


# Proof Mass Magnetic Properties

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- From Stanford measurements we find that a magnetic susceptibility of  $\chi = 1.7 \times 10^{-5}$  is achievable in a full scale PM.
  - $3 \times 10^{-6}$  previously assumed in the error budget.
- Full sized sample had a magnetic moment of  $\leq 12 \text{ nA m}^2$ .
  - $20 \text{ nA m}^2$  assumed in the error budget.

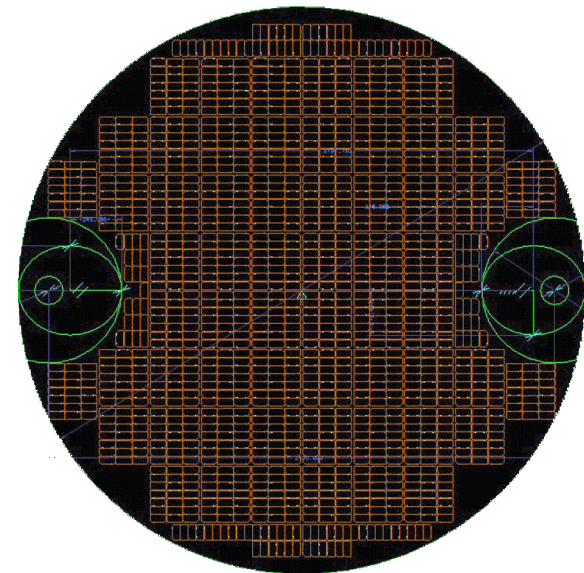
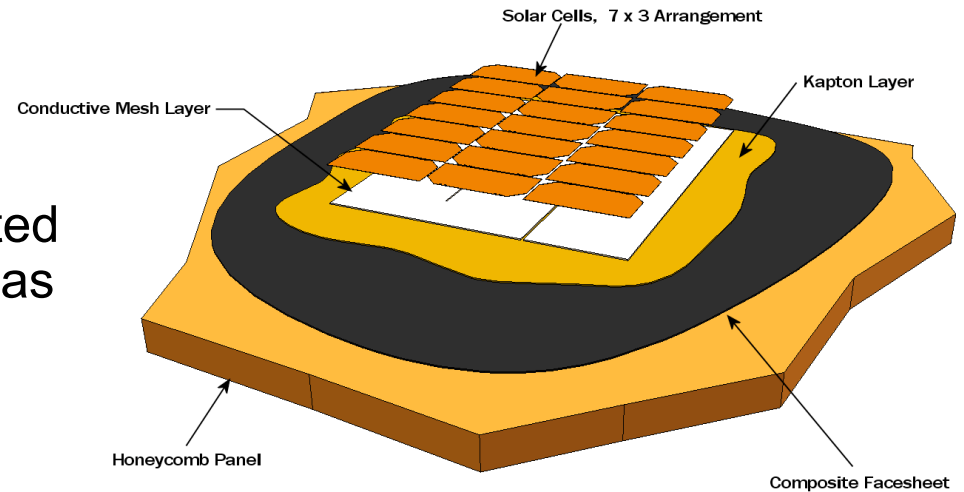




# Achieving Magnetic Performance

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- Minimize PM magnetic properties.
- Minimize use of magnetic material.
- Permanent magnets can be compensated with oppositely oriented duplicate such as the cold spare.
- Remaining permanent magnets can be shielded with METGLAS (Metglas Solutions, Inc) or VITROVAC (Vacuumschmelze).
- Backwire solar array.
- Use twisted pair for all wiring.
- Eliminate current loops in power system using star or single point grounding.
- No primary supply currents should be allowed to flow through the spacecraft structure.
- Small thermal gradients.

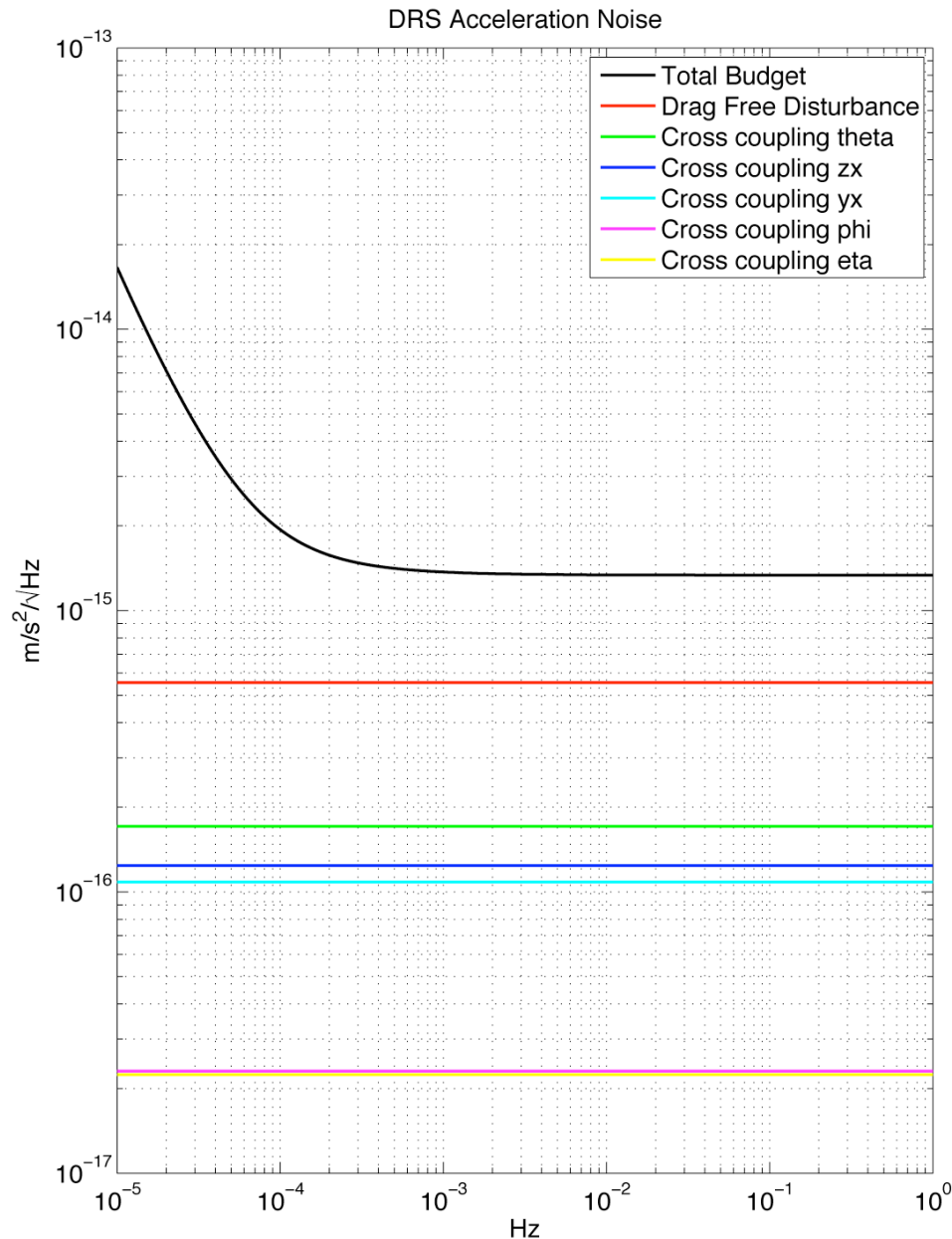






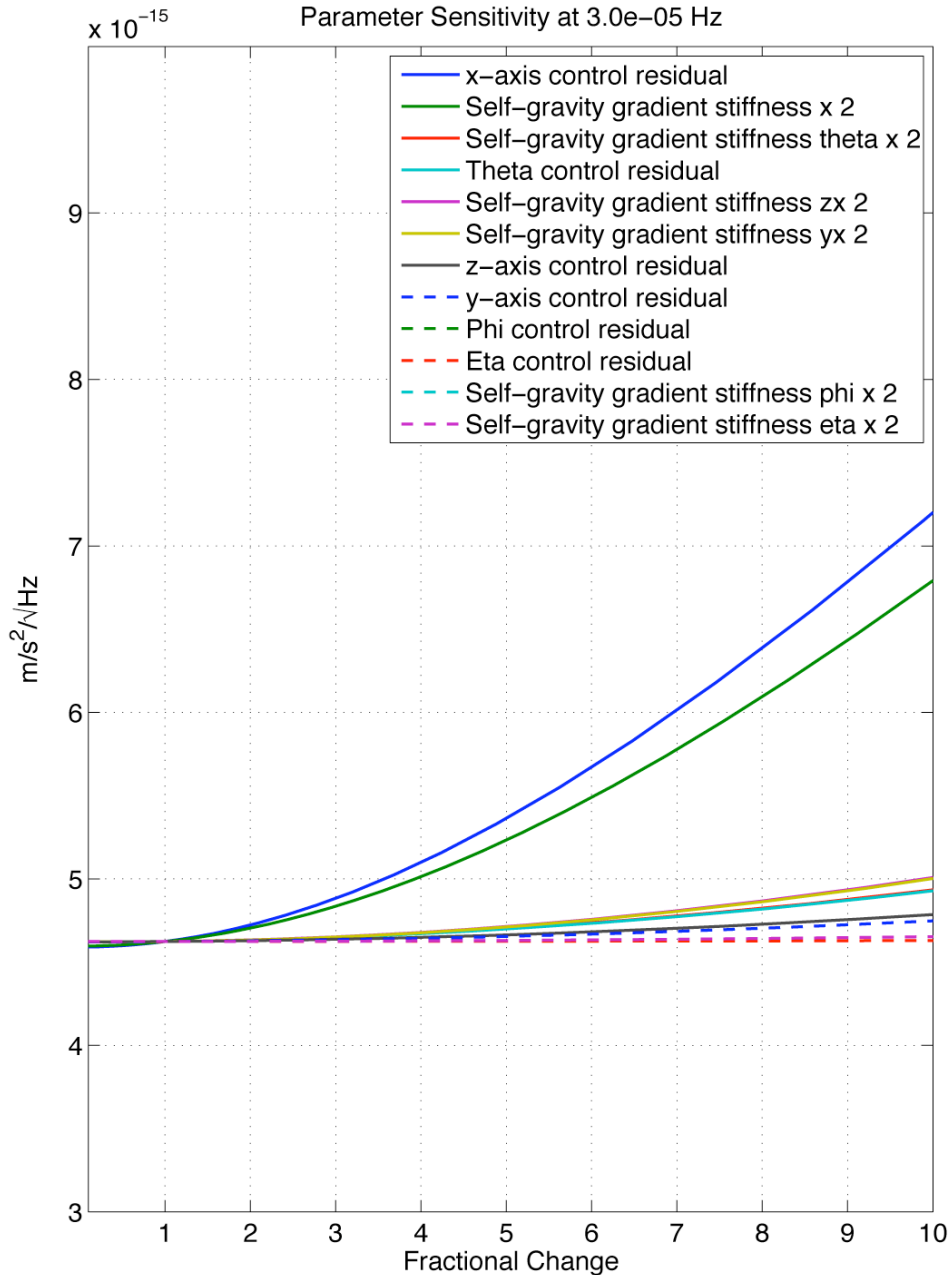
# Spacecraft - PM Coupling

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- Residual S/C motion will couple to PM through stiffness.
- Off-diagonal stiffness terms will cross-couple S/C motion to sensitive axis.
- Self-gravity gradient dominates stiffness budget.

Description	Budget ( $\text{s}^{-2}$ )
Self-Gravity Gradient	1.00E-07
Sensing Stiffness	4.34E-08
Rotation Actuation Stiffness	1.64E-08
Magnetic Stiffness	1.18E-08
DC Voltage Stiffness	3.59E-09



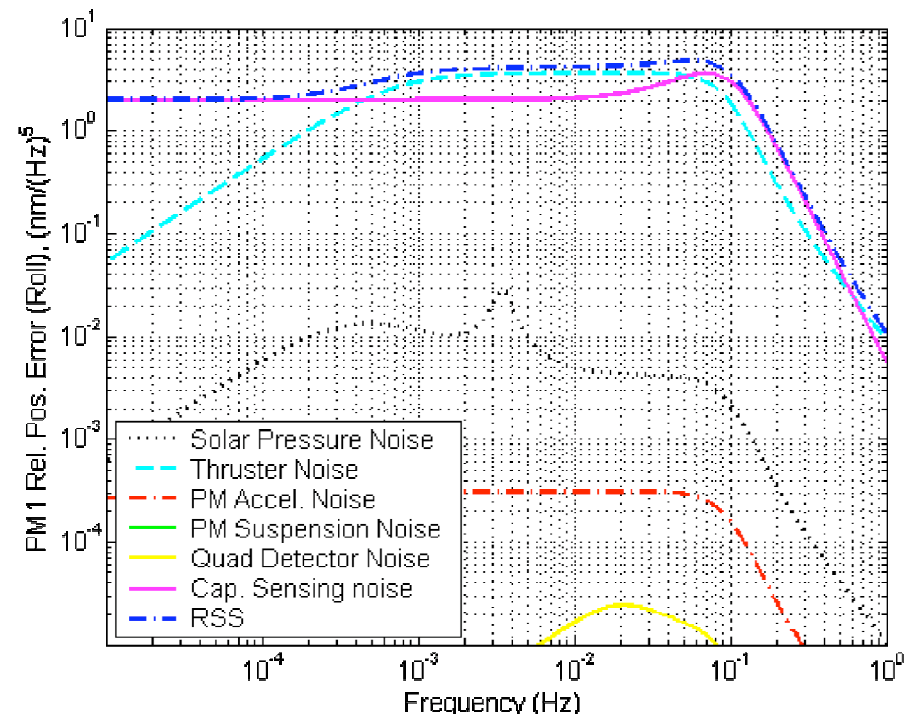
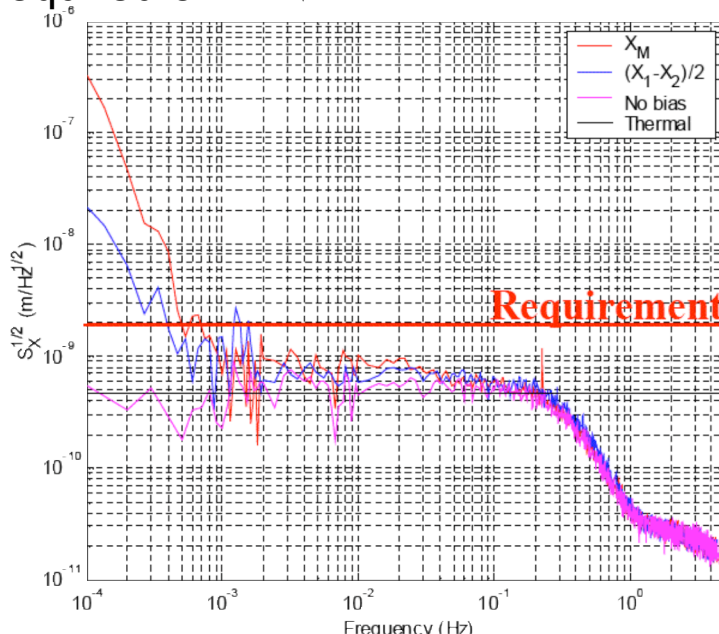
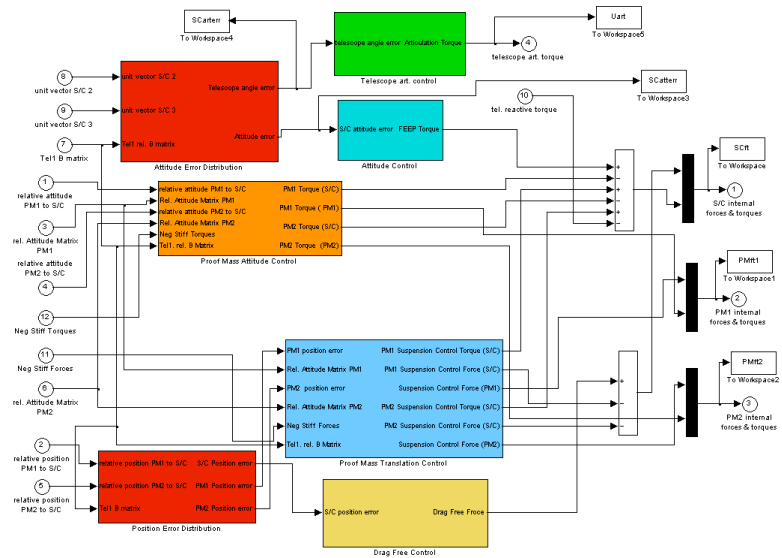
Description	Budget	Units	Sensitivity
x-axis control residual	5E-09	m/ $\sqrt{Hz}$	0.014
Self-gravity gradient stiffness x	1E-07	s <sup>-2</sup>	0.012
Self-gravity gradient stiffness theta x	5E-08	s <sup>-2</sup>	0.001
theta control residual	2E-07	rad/ $\sqrt{Hz}$	0.001
Self-gravity gradient stiffness zx	2E-08	s <sup>-2</sup>	0.001
Self-gravity gradient stiffness yx	2E-08	s <sup>-2</sup>	0.001
z-axis control residual	1E-08	m/ $\sqrt{Hz}$	0.001
y-axis control residual	1E-08	m/ $\sqrt{Hz}$	0.001
Self-gravity gradient stiffness phi x	5E-08	s <sup>-2</sup>	0.000
Self-gravity gradient stiffness eta x	5E-08	s <sup>-2</sup>	0.000
phi control residual	5E-08	rad/ $\sqrt{Hz}$	0.000
eta control residual	5E-08	rad/ $\sqrt{Hz}$	0.000



# Control Law Performance

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- Full LISA DRS model: S/C (6-DOF), two Proof Masses (6-DOF each), and telescope articulation for total of 19-DOF.
- Three S/C combined gives 57-DOF.
- Nonlinear translational and rotational kinematics and dynamics.
- Preliminary designs completed for all DRS control systems.
- Control is straightforward and simulations predicts position control better than required 5 nm/ $\sqrt{\text{Hz}}$ .



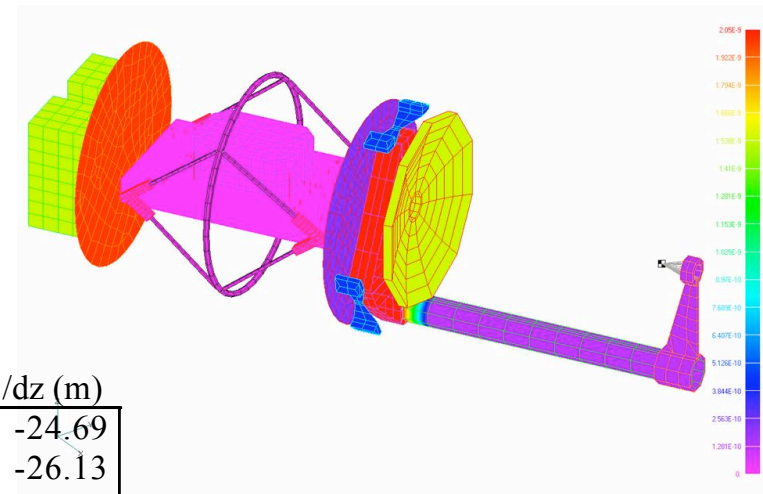
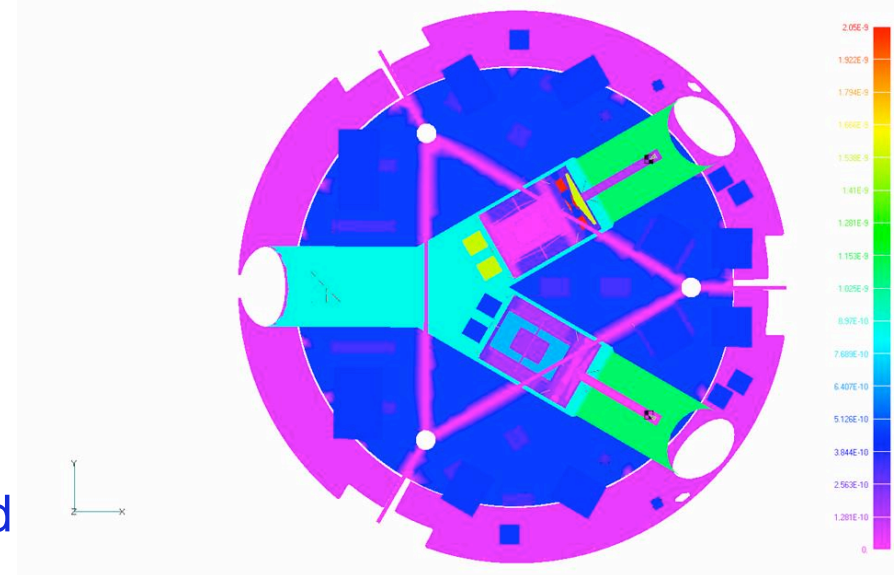




# Self-Gravity Gradient

Beyond Einstein: From the Big Bang to Black Holes

- Self-gravity gradient is the dominant stiffness term.
- Self-gravity tool developed to aid in design and verification.
  - Computes forces, moments, and gradients on each proof mass,
  - Tools accept distorted and undistorted cases
  - Visualization capability to map contributions.
- Analysis of unoptimized design within 4x of budget.



	/dx (m)	/dy (m)	/dz (m)	/dx (m)	/dy (m)	/dz (m)
dAx (1/s <sup>2</sup> x 10 <sup>-10</sup> ) =	-1264.32	85.39	-25.74	-1258.04	-104.25	-24.69
dAy (1/s <sup>2</sup> x 10 <sup>-10</sup> ) =	85.39	1669.91	7.20	-104.25	1666.05	-26.13
dAz (1/s <sup>2</sup> x 10 <sup>-10</sup> ) =	-25.74	7.19	-405.60	-24.69	-26.13	-408.01
dαx (r/s <sup>2</sup> /m x 10 <sup>-10</sup> ) =	1.81	1137.84	49.92	1.42	1138.13	50.69
dαy (r/s <sup>2</sup> /m x 10 <sup>-10</sup> ) =	-300.77	-0.70	-9.01	-300.88	-0.45	-6.62
dαz (r/s <sup>2</sup> /m x 10 <sup>-10</sup> ) =	-1.73	-8.19	-1.11	-0.16	-4.63	-0.97



# LISA

## Achieving Spacecraft - PM Coupling Performance

Beyond Einstein: From the Big Bang to Black Holes



### Improve sensor sensitivity

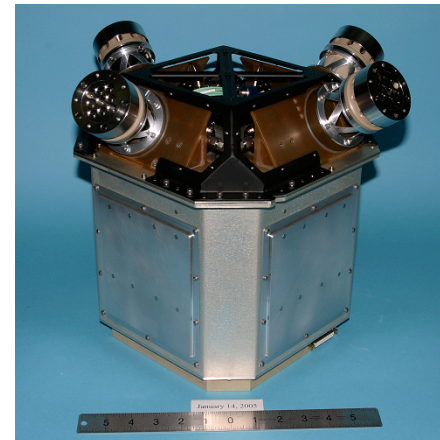
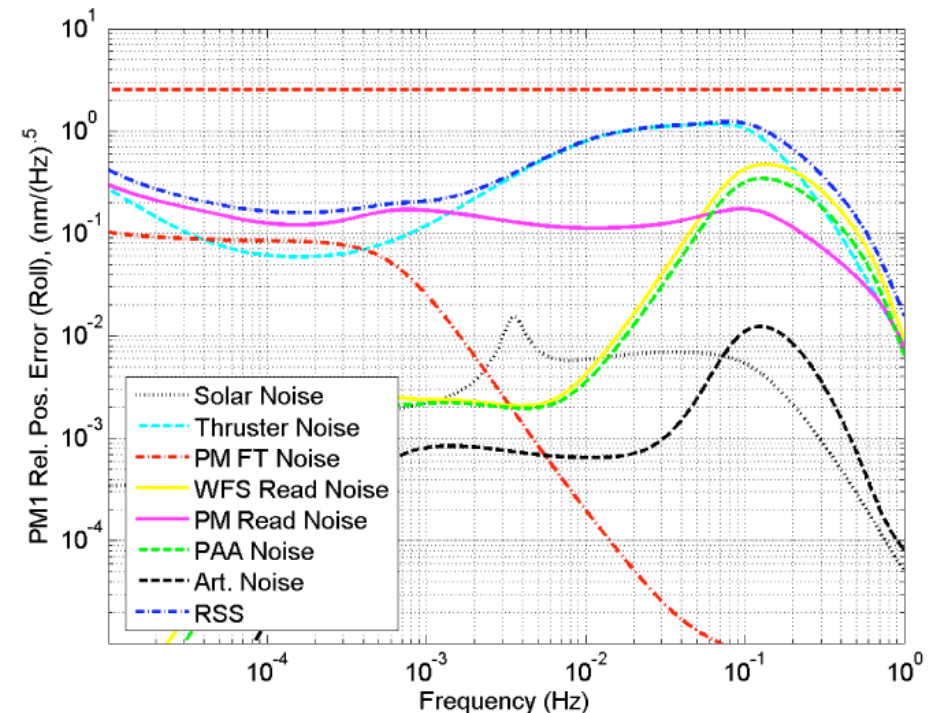
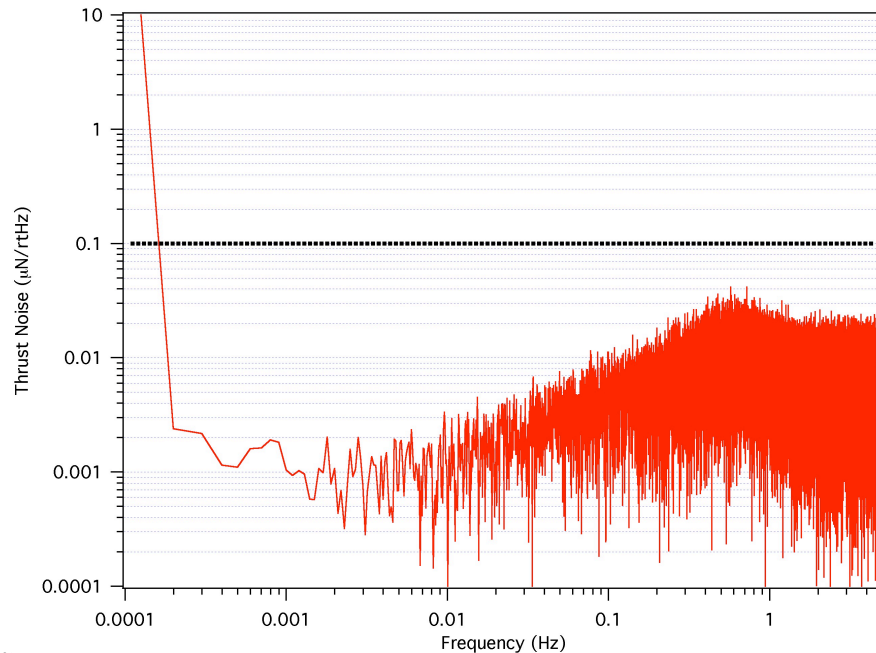
- Simulation using optical sensing predicts position control of  $0.18 \text{ nm}/\sqrt{\text{Hz}}$  @  $0.1 \text{ mHz}$  (more than 10x better than budget).



### Use low-noise thrusters



### Careful tracking of all sciencecraft mass.





# Summary



*Beyond Einstein: From the Big Bang to Black Holes*

- The very low end of the LISA frequency band has the potential for exciting science.
- Pushing the low-frequency sensitivity will increase the precision of locating a source on the sky for follow-up observations.
  - LISA will measure the absolute distance and an electromagnetic identification of the source measures the redshift enabling us to map dark energy very far back in time with almost no interpretation problems.
- Many design options are available to improve low-frequency performance.
- Greatest challenge at low-frequency is verification of performance on-ground. Reliance on modeling may be heavy.